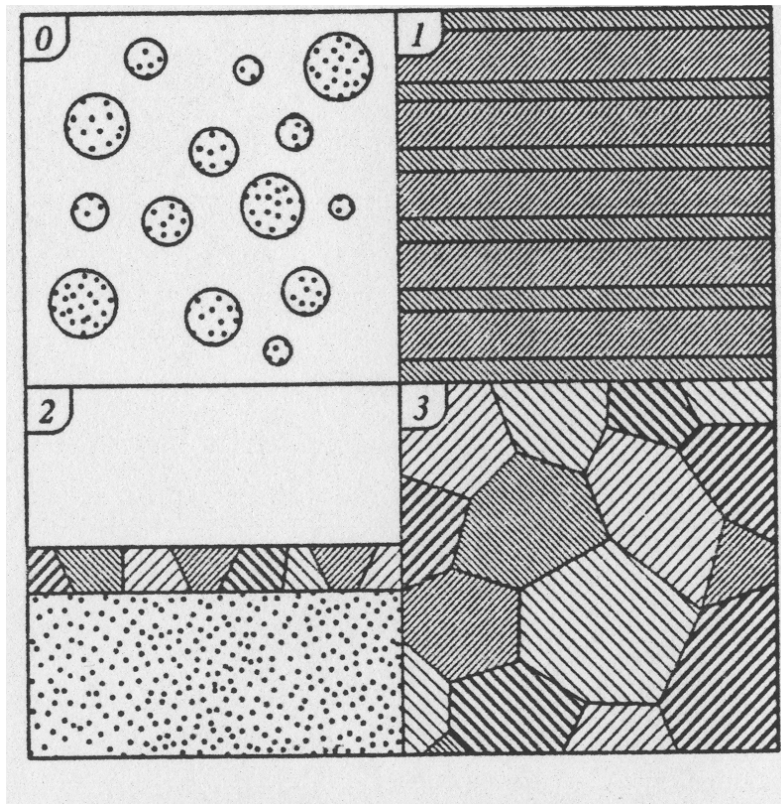


**DIFFRACTION STUDIES OF ULTRAFINE POWDERS  
AND NANOSTRUCTURED MATERIALS**

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*Boriskov Institute of Catalysis SB RAS  
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CLASSIFICATION OF NANOSTRUCTURES  
(Siegel R.W. In Proc. of NATO ASI, 1993. V.233, P.509)



- *0D Nanostructures*
- *1D Nanostructures*
- *2D Nanostructures*
- *3D Nanostructures*

## **X-ray diffractin analysis of nanocrystals**

1. Atomic structure of nanoparticles (nanoblocks).
2. Shape of nanoparticles (nanoblocks).
3. Average particle size and size distribution parameters
4. Nanostructure: stacking of blocks and structure of boundaries

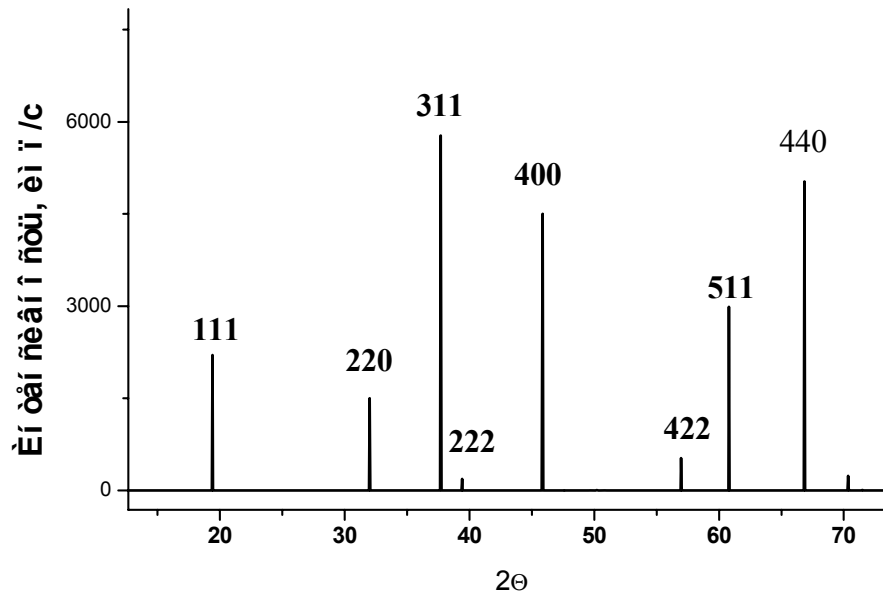
# The fundamental equations of X-ray structural analysis of polycrystals

*(model of an infinite perfect crystal)*

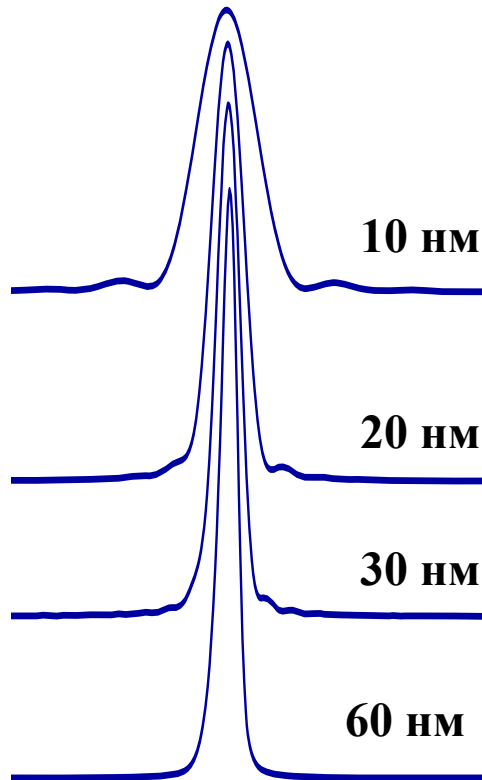
$$2d_{hkl} \sin \theta = n\lambda$$

$$I_{hkl} = kLPGF_{hkl}^2$$

$$F_{hkl} = \sum_j^N n_j T_j f_j e^{2\pi i(hx_j + ky_j + lz_j)}$$



## Broadening of the diffraction peaks due to the small size of nanoparticles



Sherrer equation

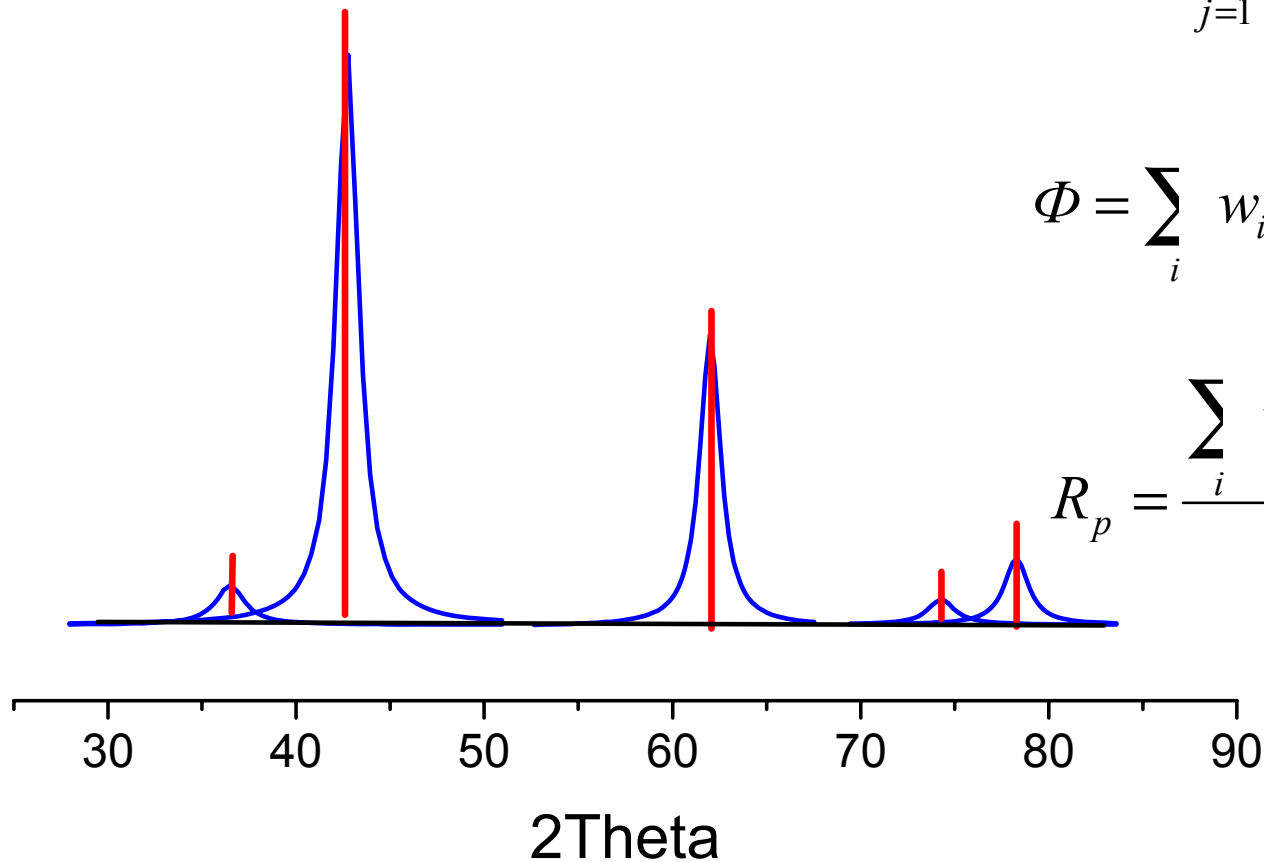
$$\beta = \frac{\lambda}{D \cos \theta}$$

**RIETVELD METHOD:**  
*crystal structure refinement*

$$y_i^T = \sum_{j=1}^N I_j \Omega_{ij} + y_i^{\text{phon}}$$

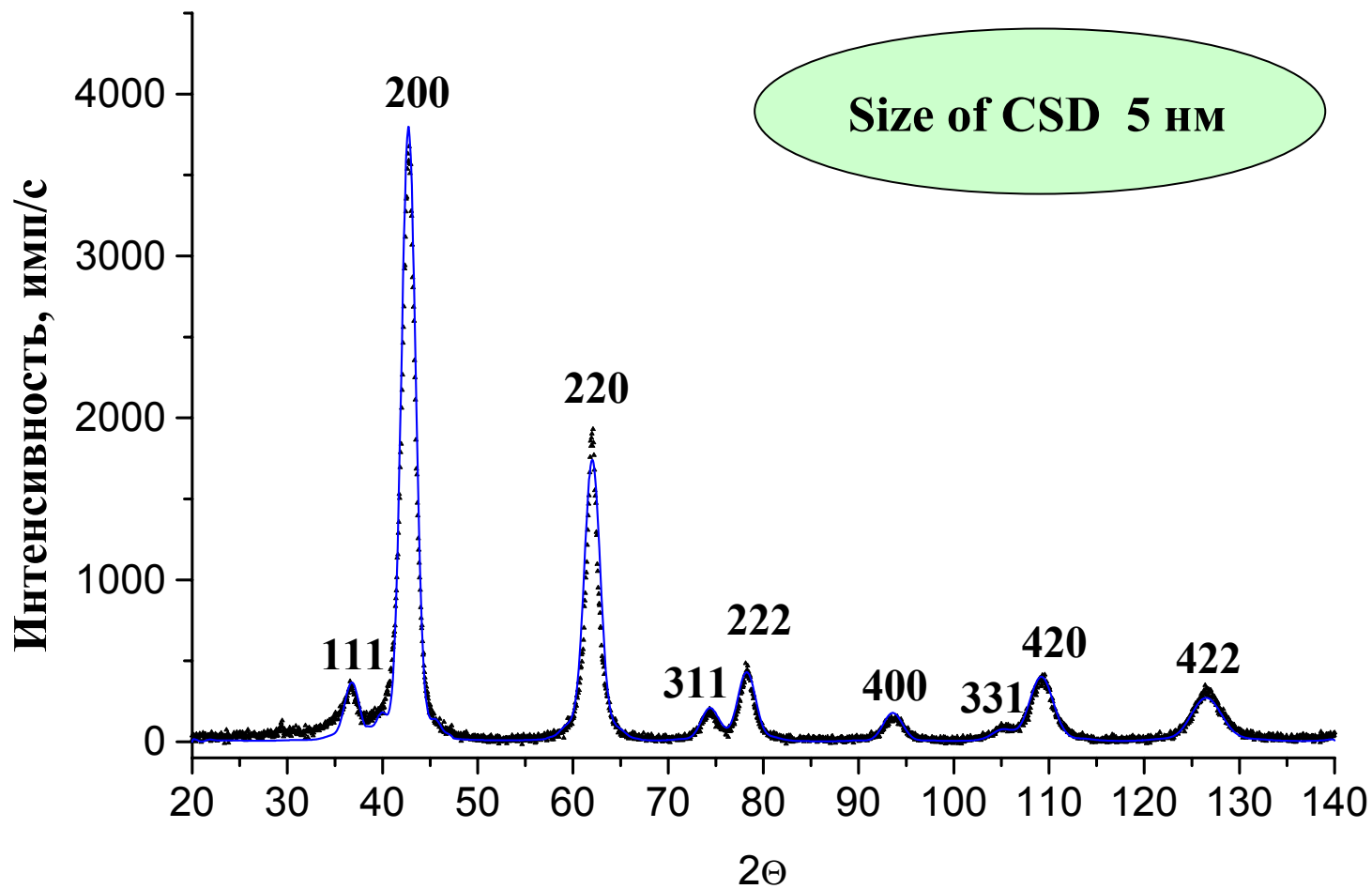
$$\Phi = \sum_i w_i (y_i^{\ominus} - ky_i^T)^2$$

$$R_p = \frac{\sum_i w_i |y_i^{\ominus} - ky_i^T|}{\sum_i w_i y_i^{\ominus}}$$

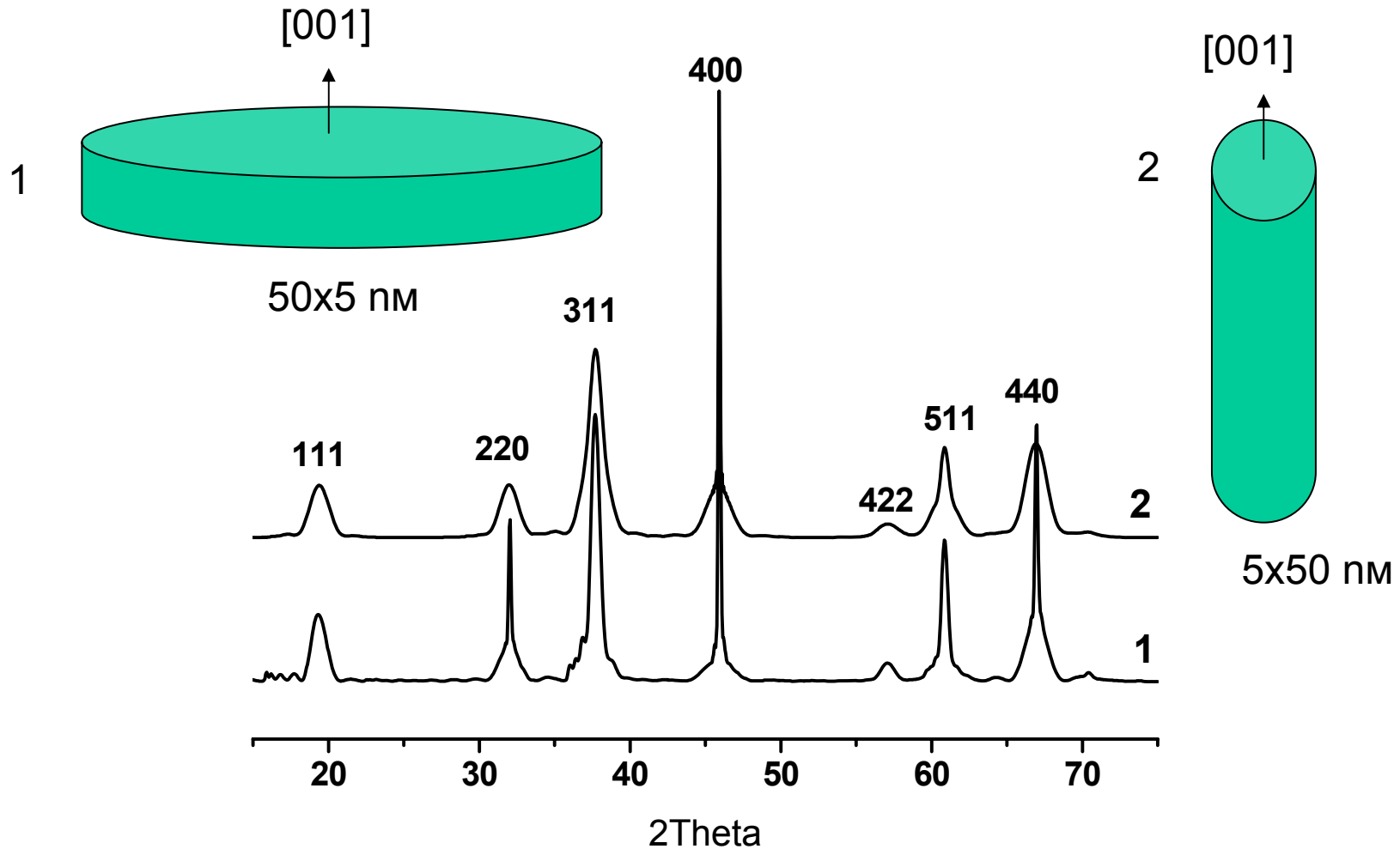


**The experimental and calculated (solid line)**

**X-ray diffraction patterns of MgO.  $R_p=7.2\%$ .**

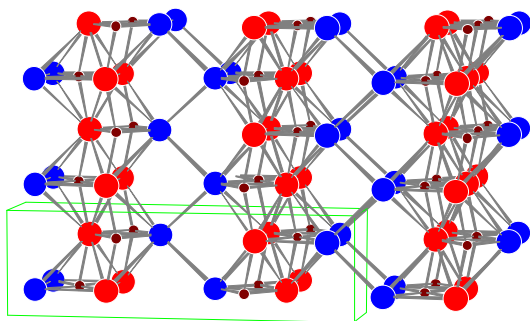
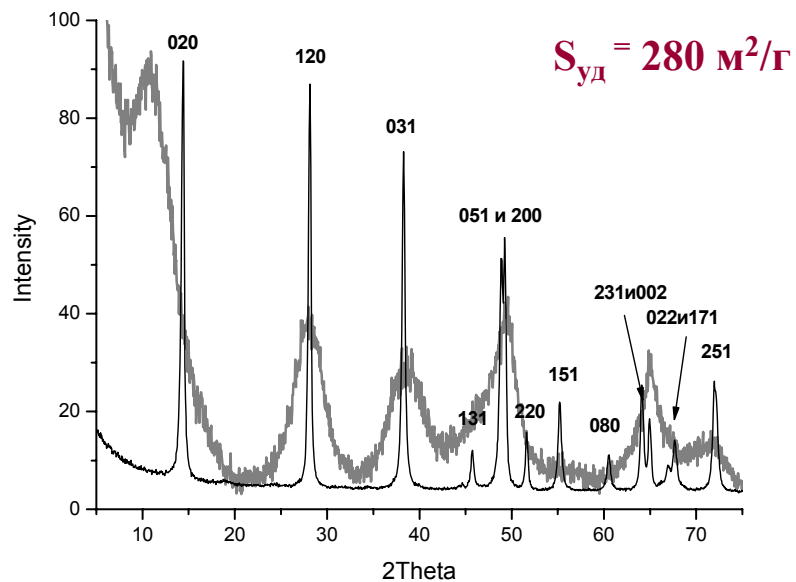


# Nanoparticles with cubic spinel structure: thin plate and cylinder

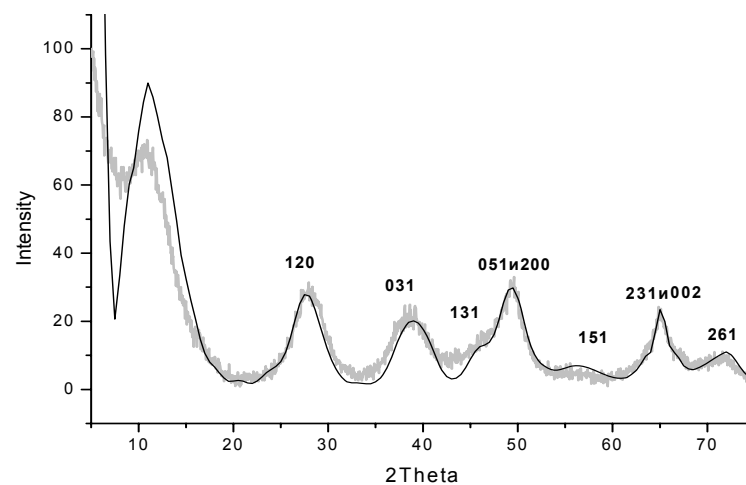
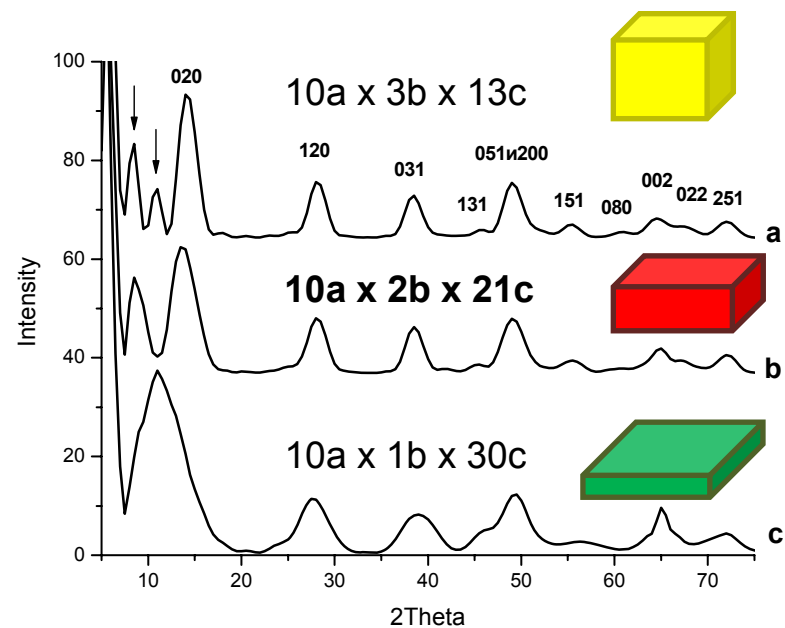




# Experimental diffraction patterns of boehmite and pseudo boehmite $\text{AlOOH} \cdot n\text{H}_2\text{O}$



## Calculations



## Debye Equation

$$I(s) = N \left[ \sum_j f_j^2 + 2 \sum_{j \neq k} \sum_k f_j f_k \cos(2\pi \vec{s} \cdot \vec{r}) \right]$$

## *Pair Distribution Function Method*

$$I(s) = N \left[ f^2(s) + \int_0^\infty 4\pi r^2 \rho(r) \frac{\sin(sr)}{sr} ds \right]$$

$$4\pi r^2 \rho(r) = 4\pi \rho_0 + \frac{2r}{\pi} \int_0^\infty si(s) \sin(sr) ds$$

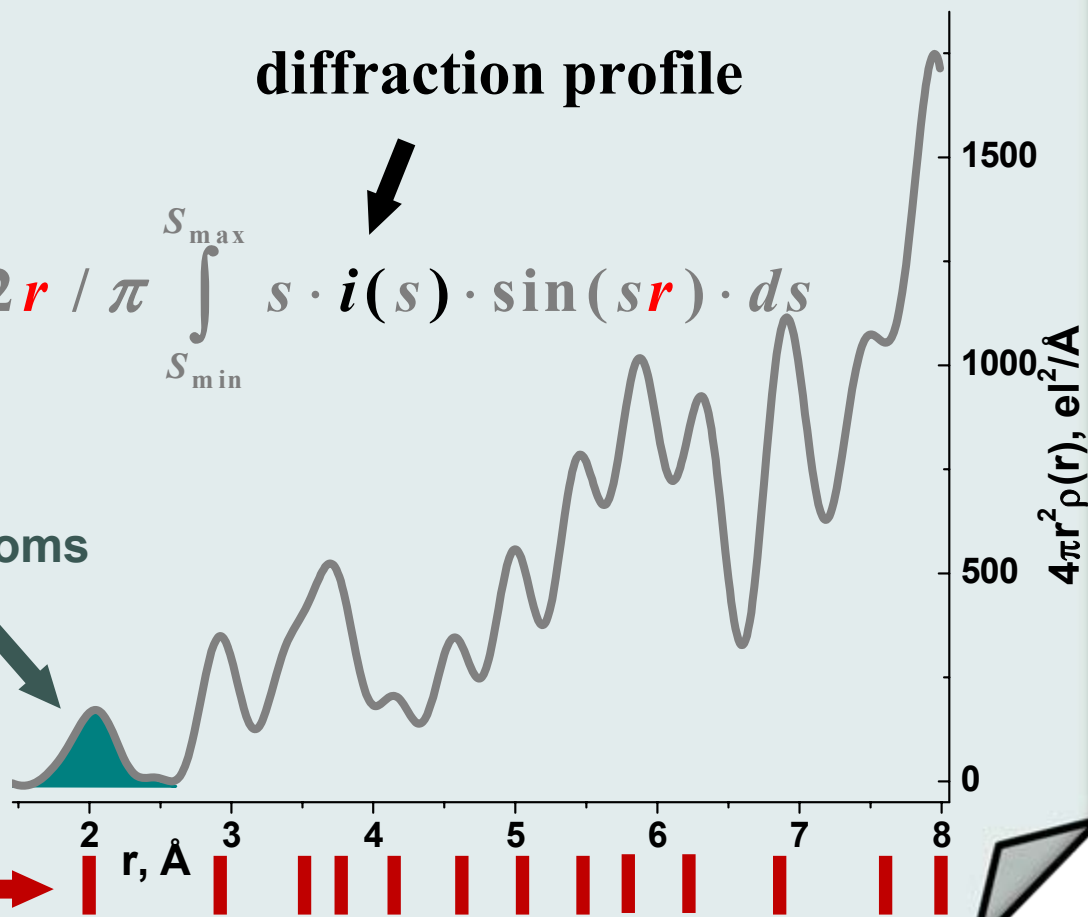
# PAIR DISTRIBUTION FUNCTION

average density

diffraction profile

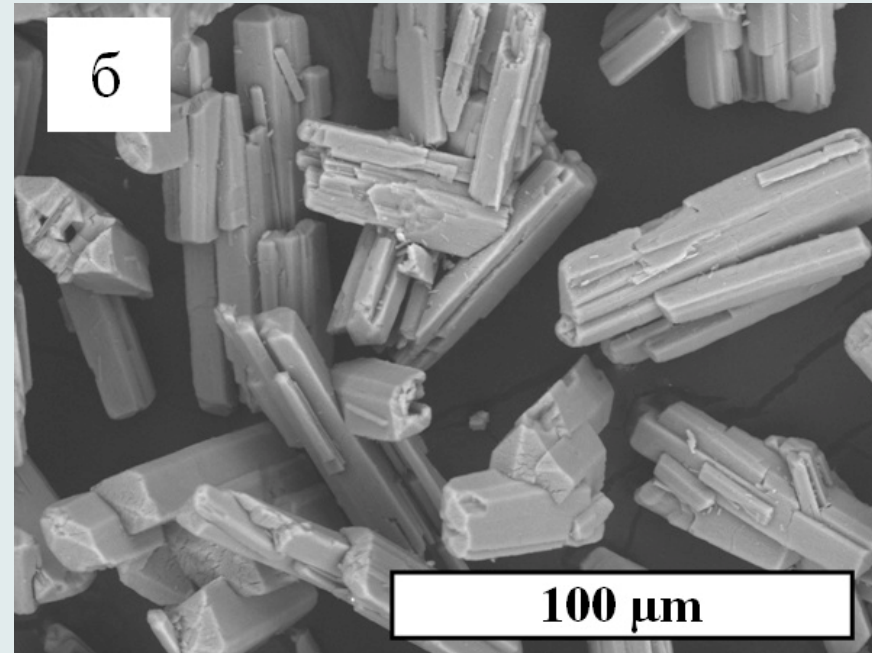
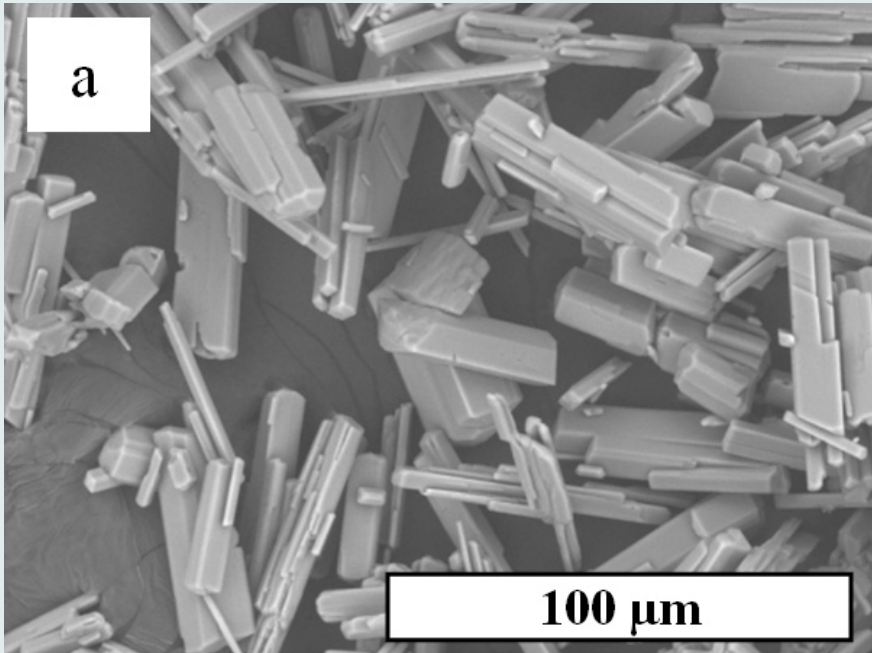
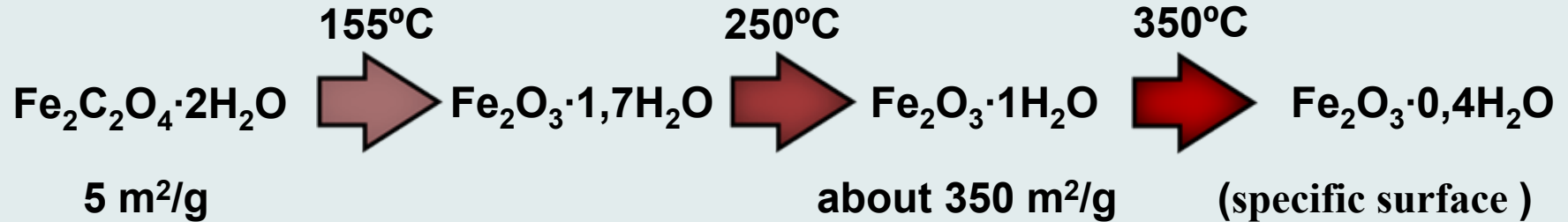
$$4\pi r^2 \rho(r) = 4\pi r^2 \rho_0 + 2r / \pi \int_{s_{\min}}^{s_{\max}} s \cdot i(s) \cdot \sin(sr) \cdot ds$$

number of atoms

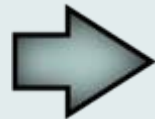


*Interatomic distances*

# Synthesis of nanostructured iron oxide

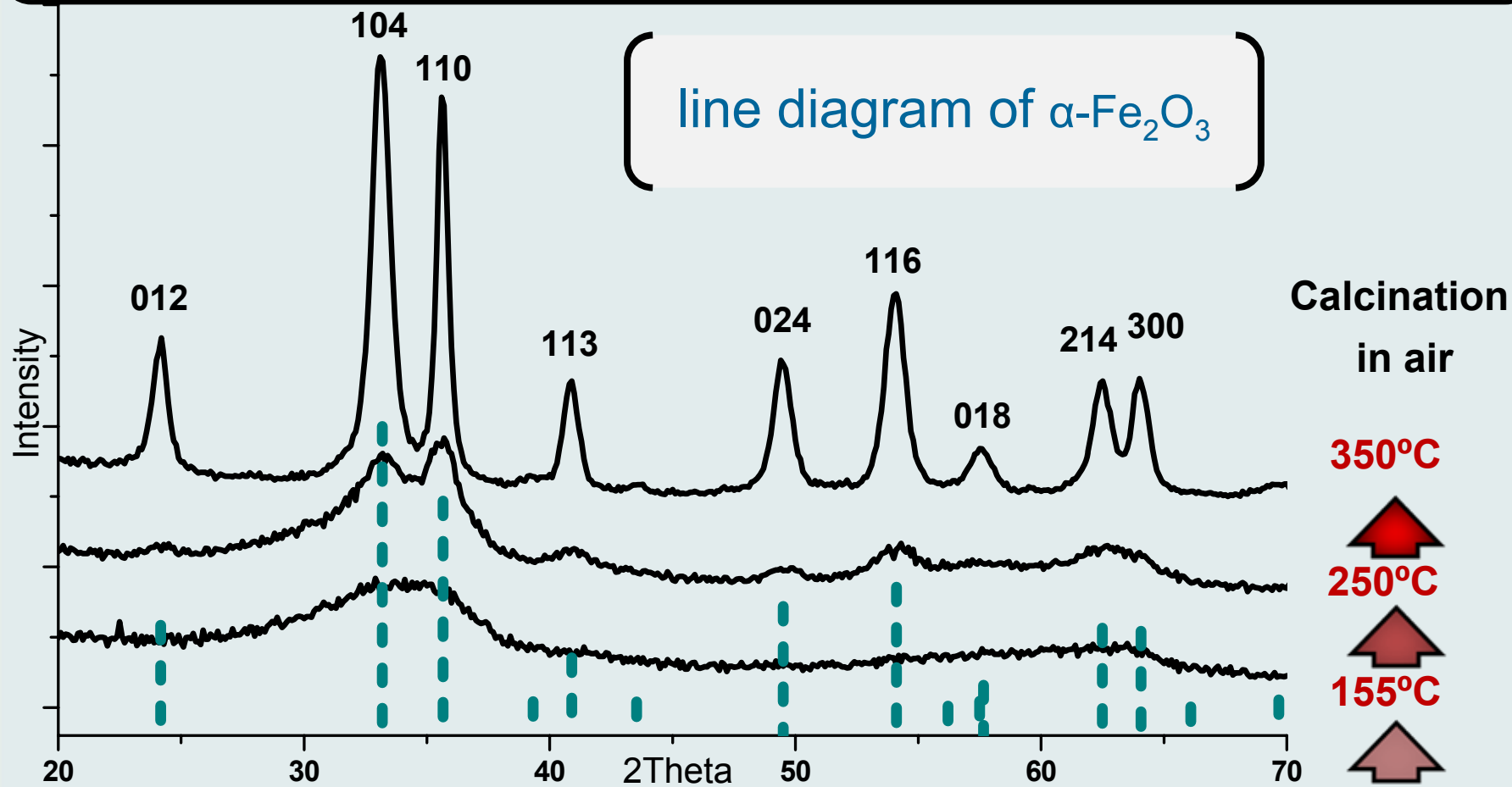


ferric oxalate dihydrate

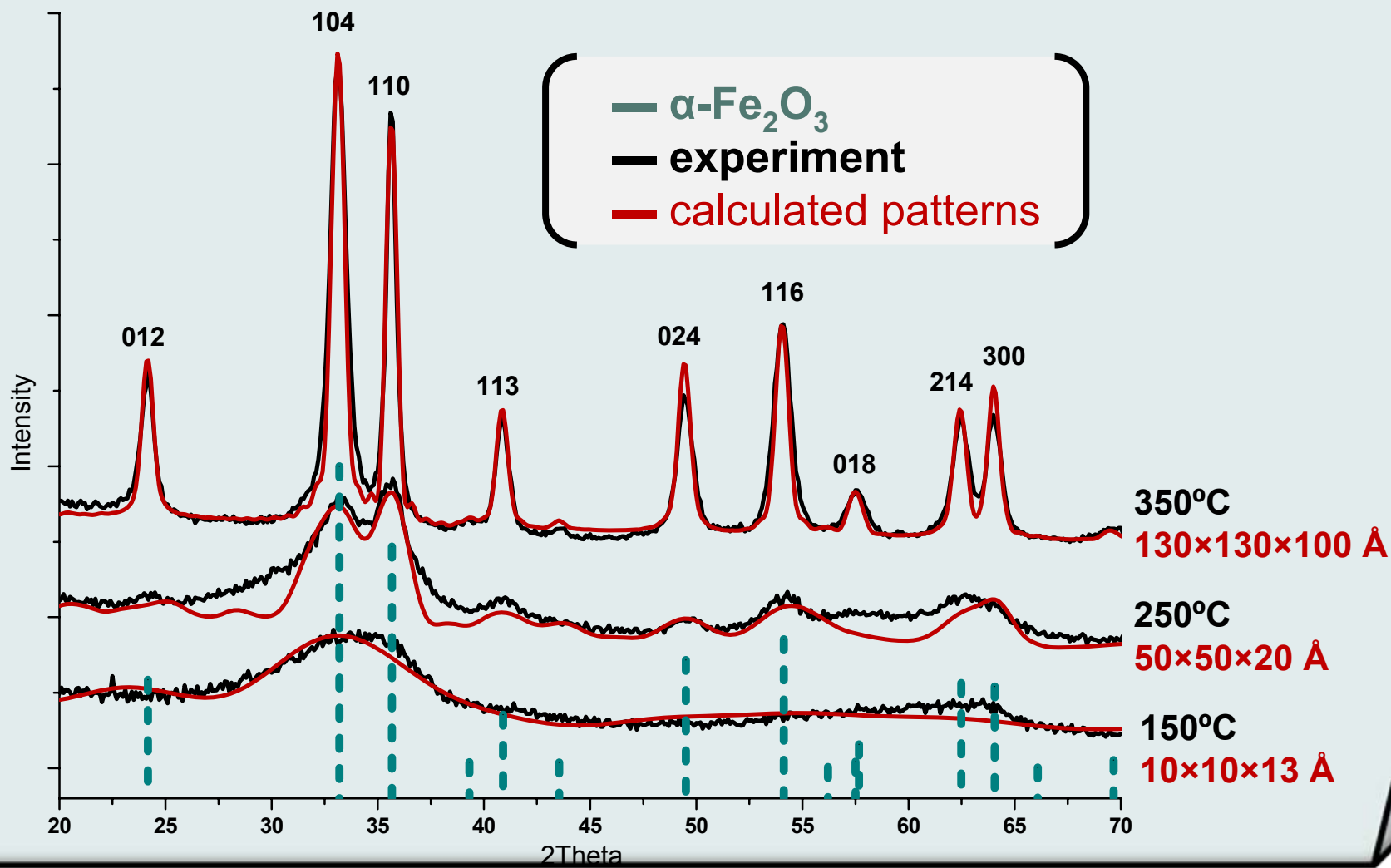


iron oxide  $\Delta V_{\text{p}}/V_{\text{p}} = 80\% \text{ pores}$

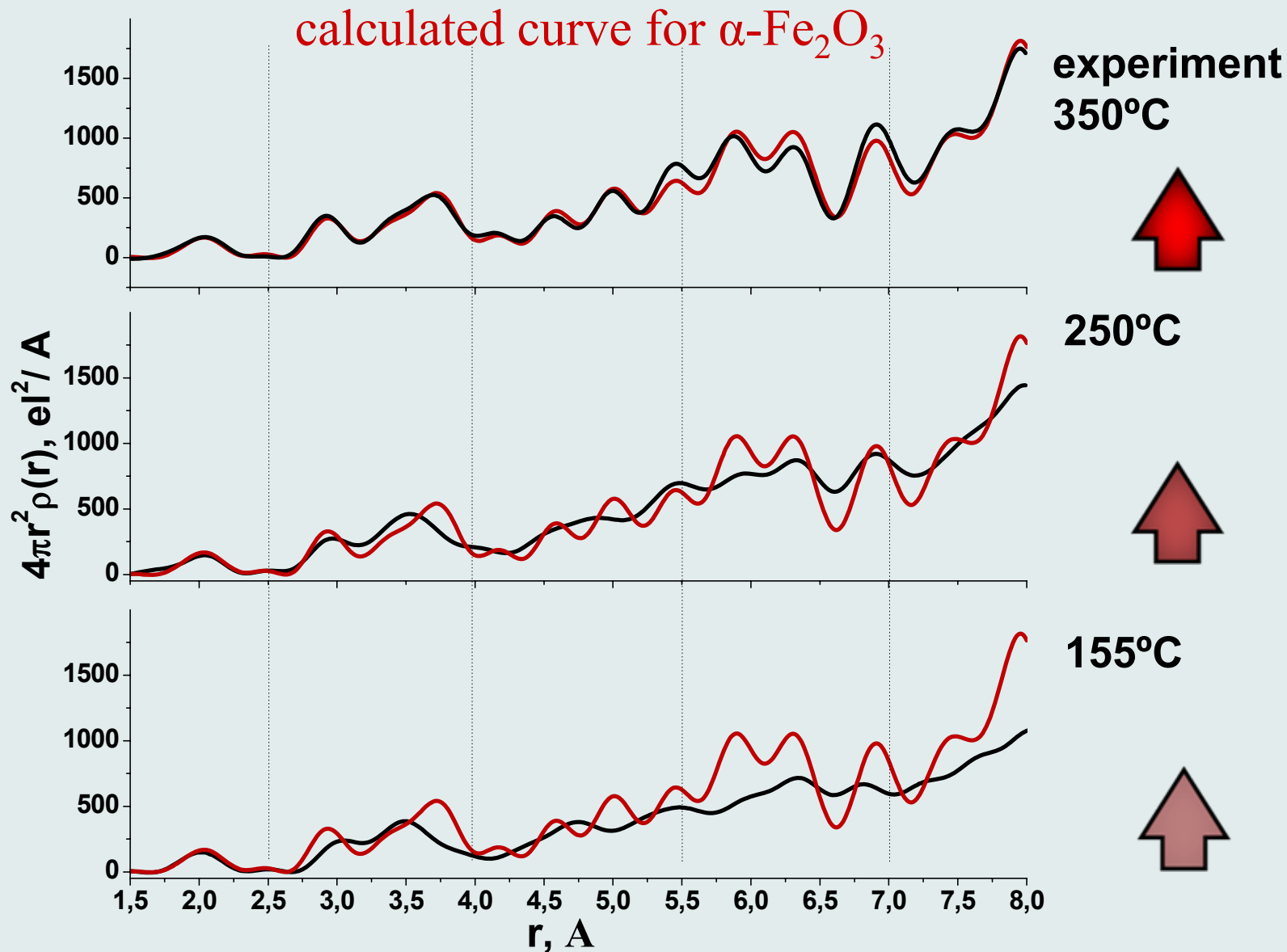
# Experimental Diffraction Patterns Of Iron Oxide



# Experimental and Calculated Diffraction Patterns (Hematite model)

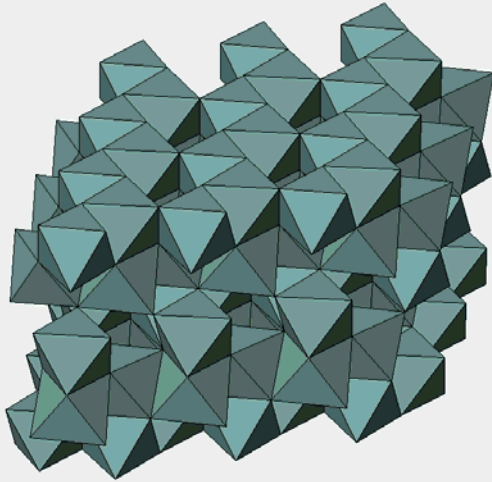


# Pair Distribution Functions of $\text{Fe}_2\text{O}_3$ samples



# Crystalline phases of iron oxide

hematite ( $\alpha\text{-Fe}_2\text{O}_3$ )



R -3 c

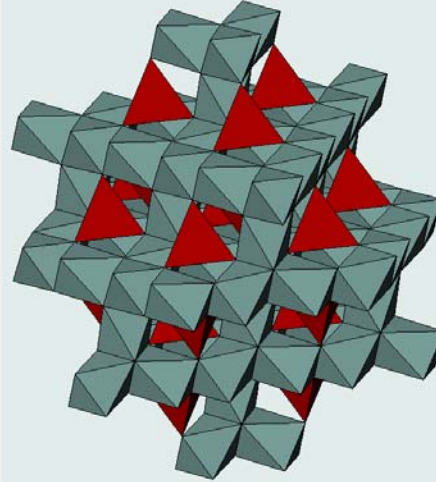
$$a = b = 5\text{\AA}$$

$$c = 13.7\text{\AA}$$

$$\alpha = \beta = 90$$

$$\gamma = 120$$

magnetite ( $\text{Fe}_3\text{O}_4$ )

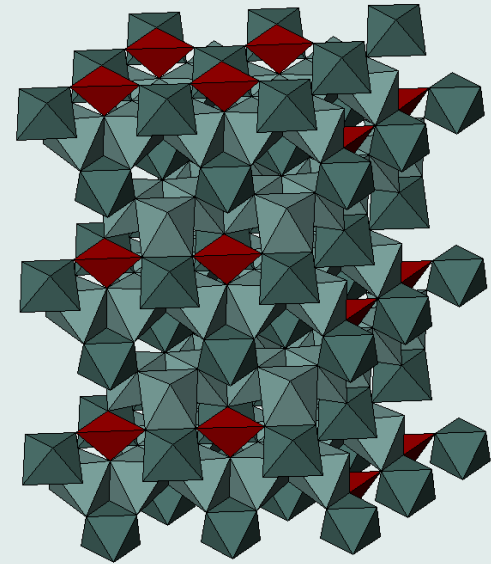


F d -3 m

$$a = b = c = 8.4\text{\AA}$$

$$\alpha = \beta = \gamma = 90$$

ferrhydrite  
 $\text{Fe}_2\text{O}_3 \cdot n\text{H}_2\text{O}$  ( $n \leq 1,8$ )



P  $6_3$  m c

$$a = b = 6\text{\AA}$$

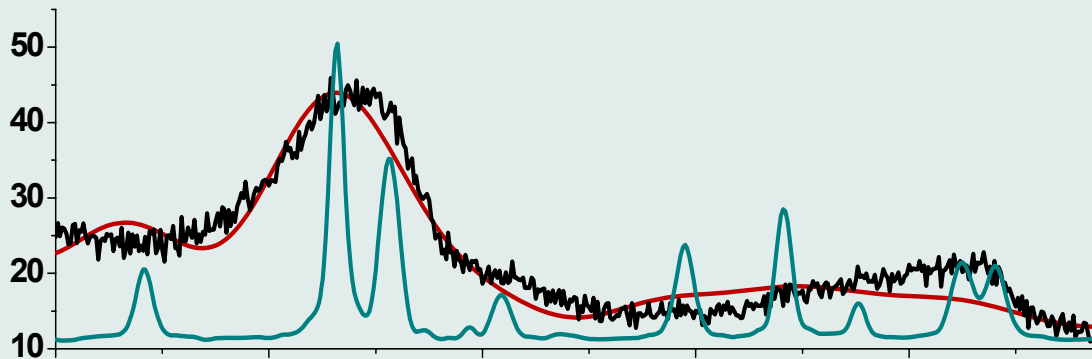
$$c = 9.1\text{\AA}$$

$$\alpha = \beta = 90$$

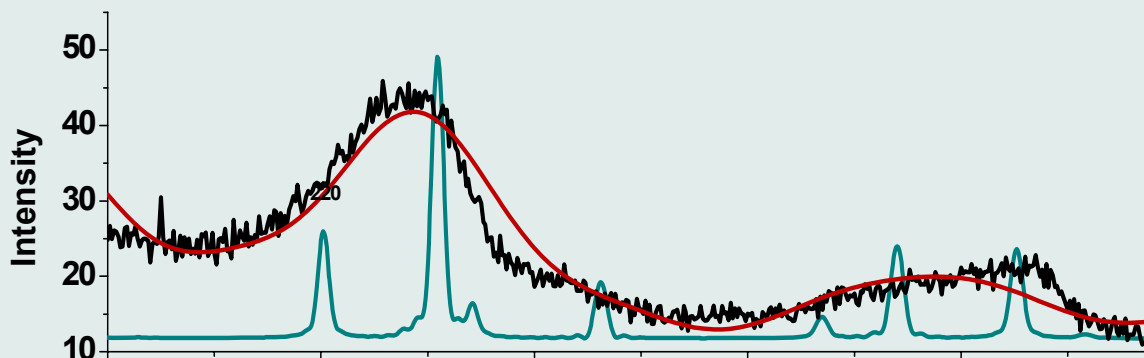
$$\gamma = 120$$



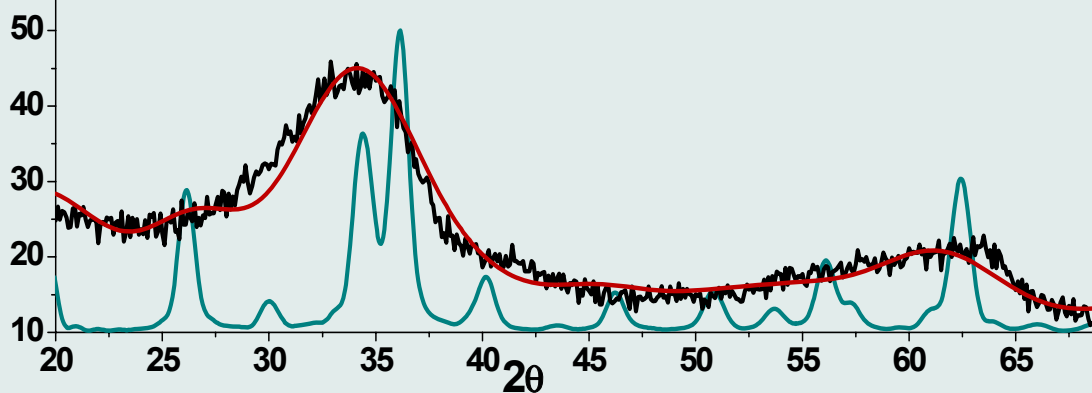
# Experimental (black) and calculated (red) diffraction patterns (150°C sample)



hematite ( $\alpha\text{-Fe}_2\text{O}_3$ )

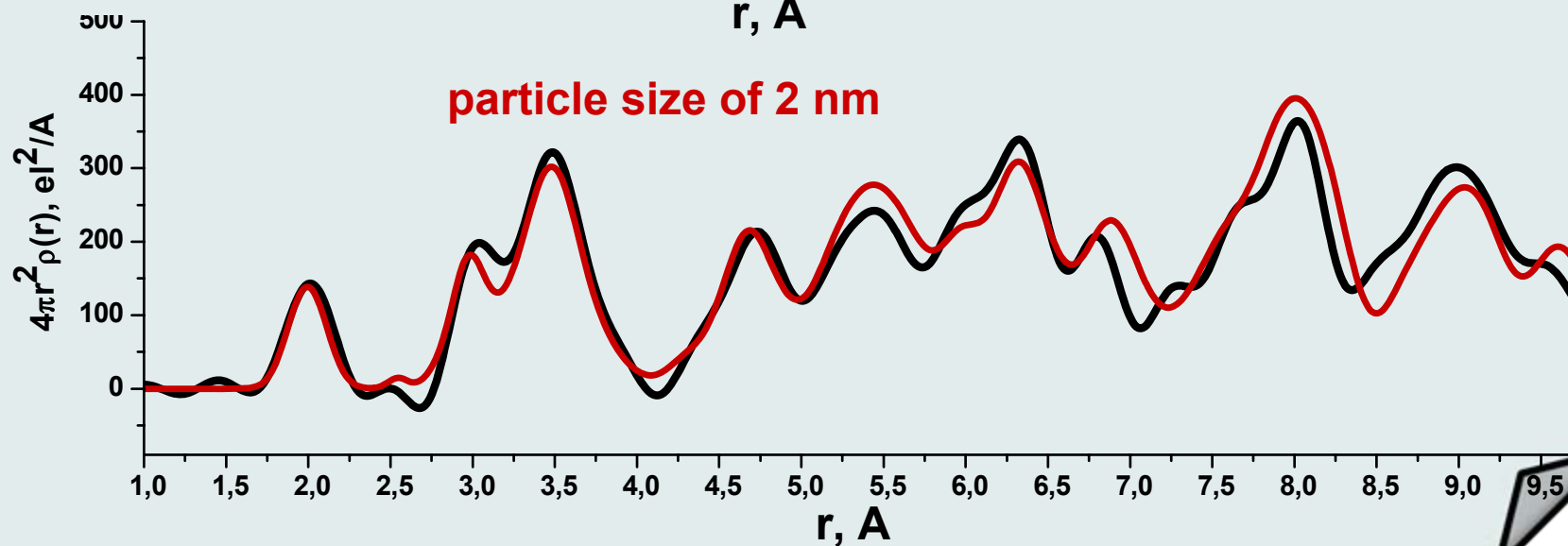
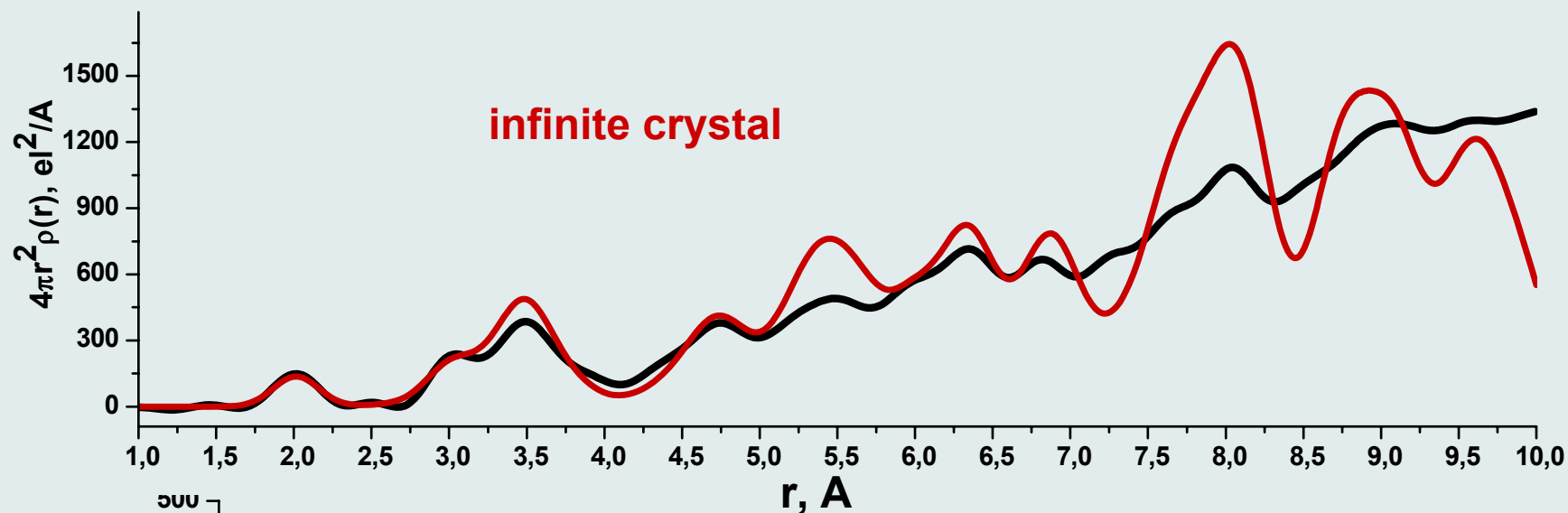


magnetite ( $\text{Fe}_3\text{O}_4$ )



ferrihydrite  
( $\text{Fe}_2\text{O}_3 \cdot n\text{H}_2\text{O}$ ,  $n \leq 2$ )

# PDF of ferrihydrite $\text{Fe}_2\text{O}_3 \cdot n\text{H}_2\text{O}$ : experimental (black) and calculated (red) curves

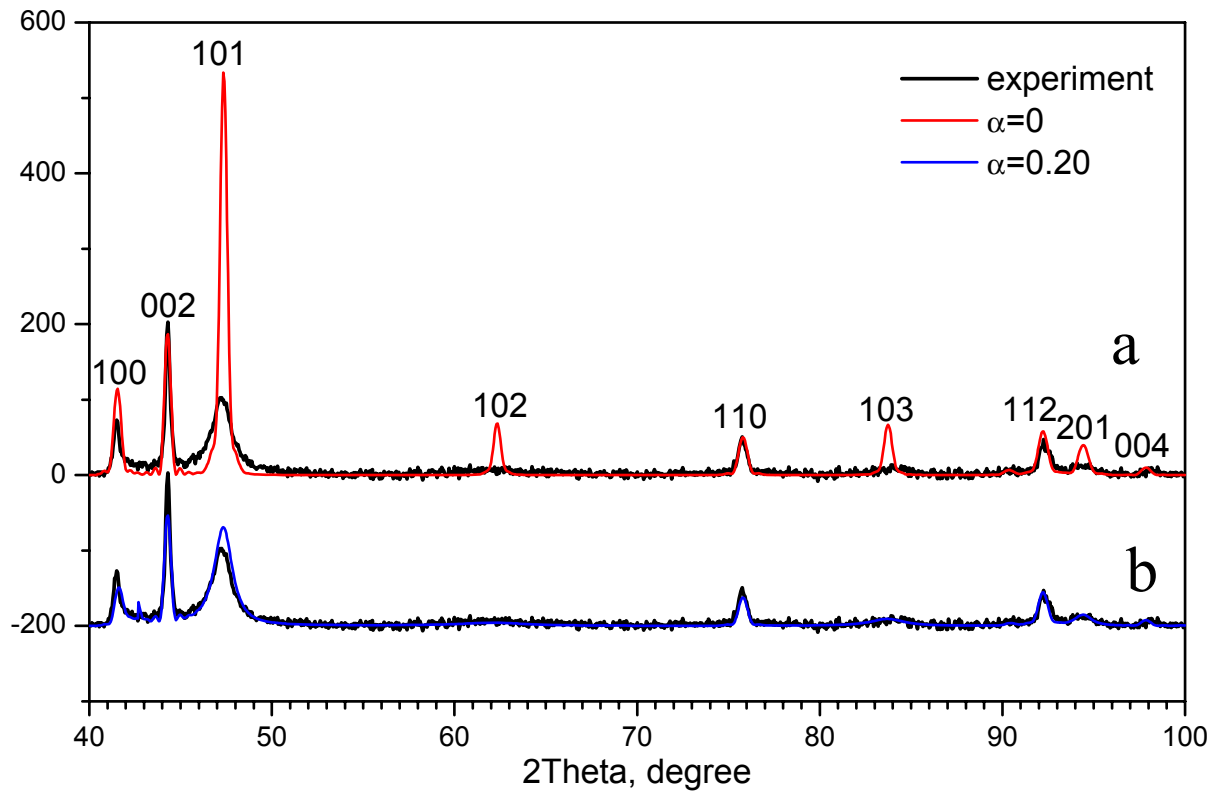


# EFFECT OF RANDOMLY DISTRIBUTED STACKING FAULTS

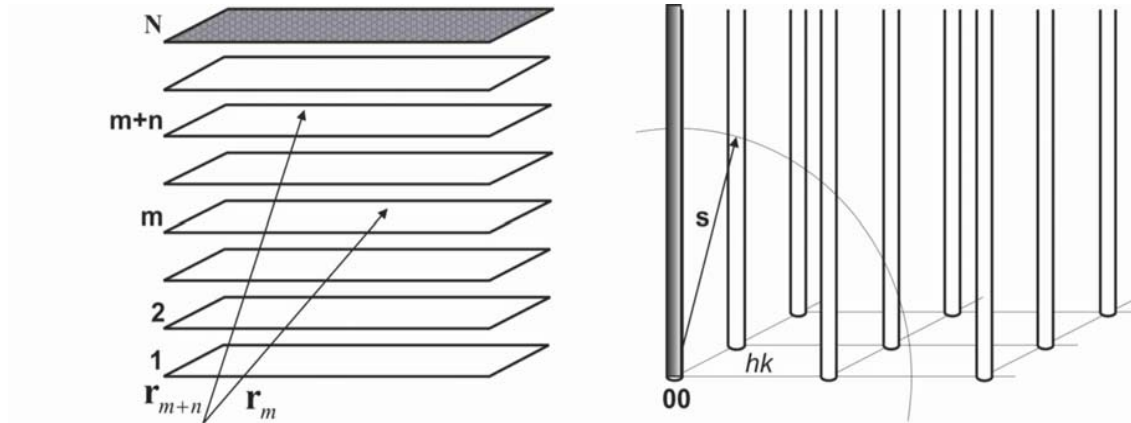
X-ray diffraction patterns of metallic hexagonal Co :

a – nanoparticles with regular crystal structure

b – nanoparticles with stacking faults (20% concentration)



# Diffraction from 1D distorted system



$$i_{hk}(l) = \frac{1}{\Omega\sigma} \left\{ \text{Trace}\mathbf{FW} + 2 \operatorname{Re} \sum_n^{N-1} \frac{N-n}{N} \text{Trace}\mathbf{FWQ}^n \right\}$$

$$i_{hk}(s) = i_{hk} G(\varepsilon_h, \varepsilon_k)$$

$$I_{hk}(s) = \frac{1}{4\pi s^2} \int_A i_{hk}(\mathbf{s}) dA$$

## Parameters of statistical model (Markov chain)

**N** - number of layers

**S, G** - short order parameters in layers position and shift

**S=0**       $w_A, w_B, w_C$

*Probability of presence of A,B,C layers*

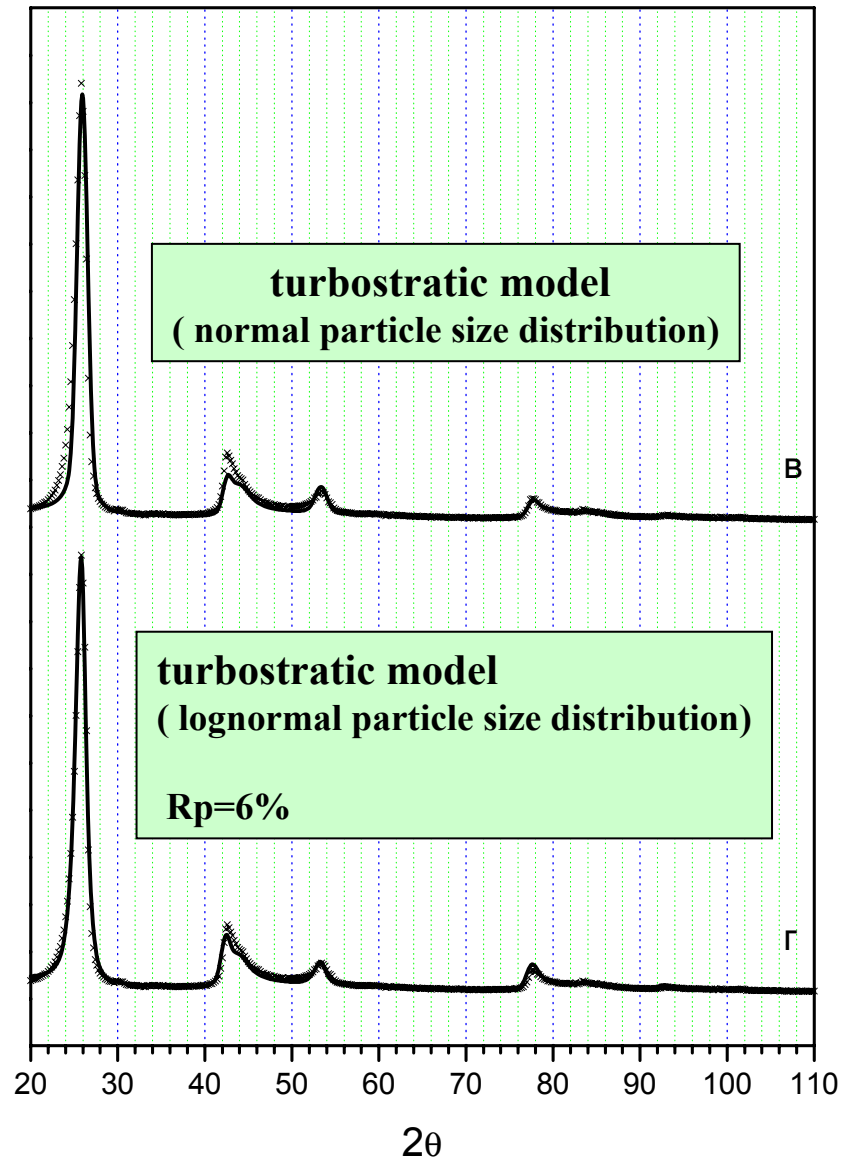
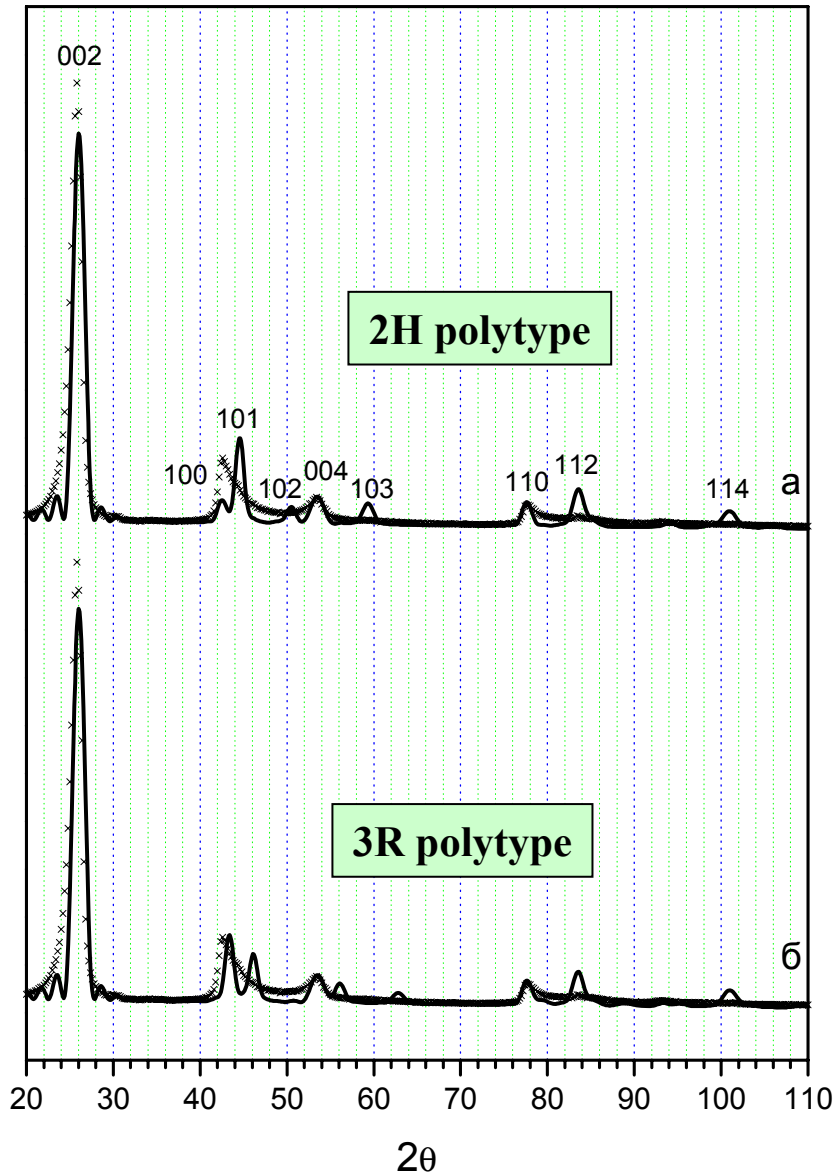
**S=1**       $w_{AA}, w_{AB}, w_{BA}, w_{BC} \dots$

*Probability of layers appearance  
after each other*

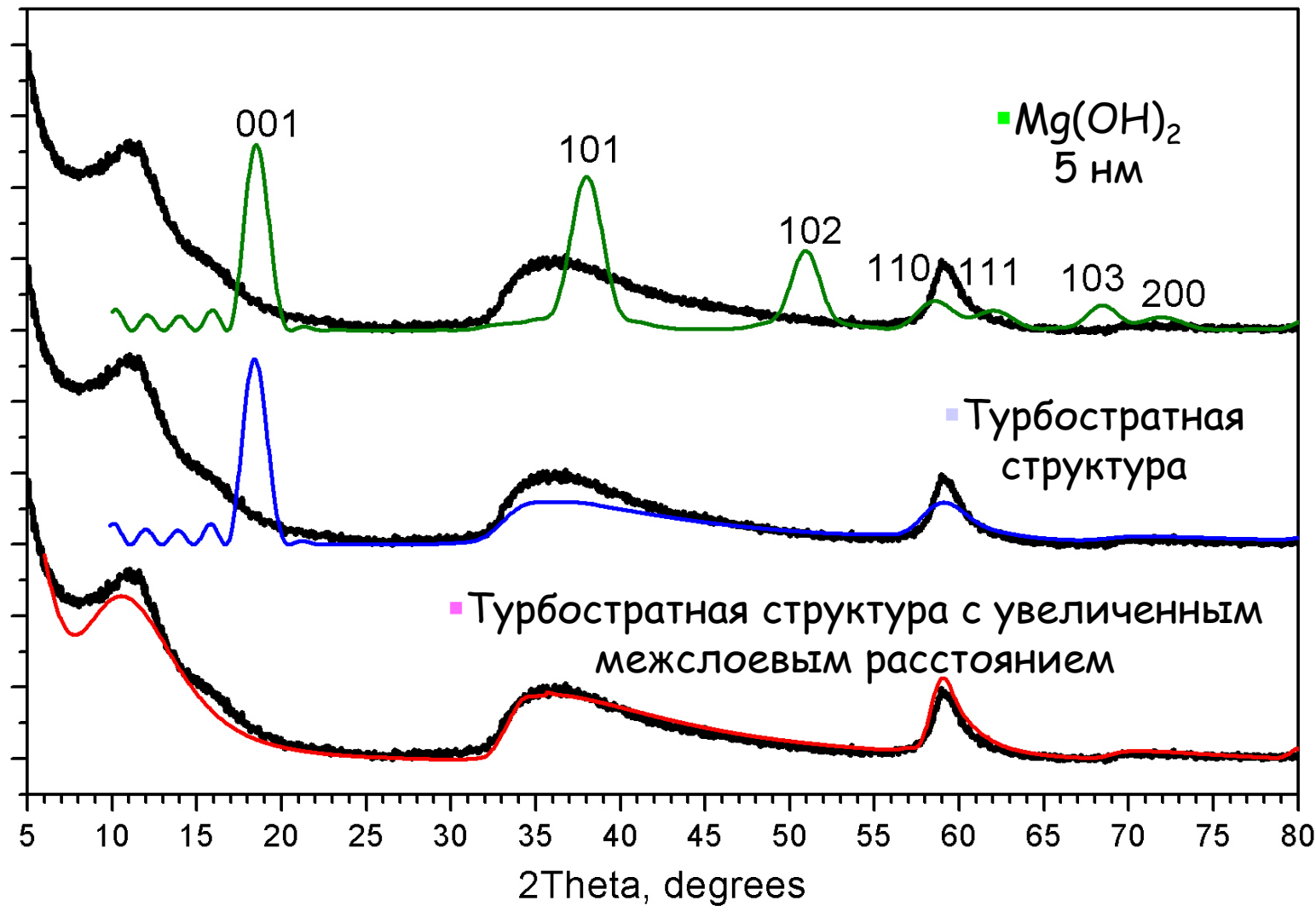
**S=2**       $w_{AAA}, w_{AAB}, w_{ABA},$

*Probabilities of appearance of A-layer  
after AA pair, B-layer after AA pair, etc.*

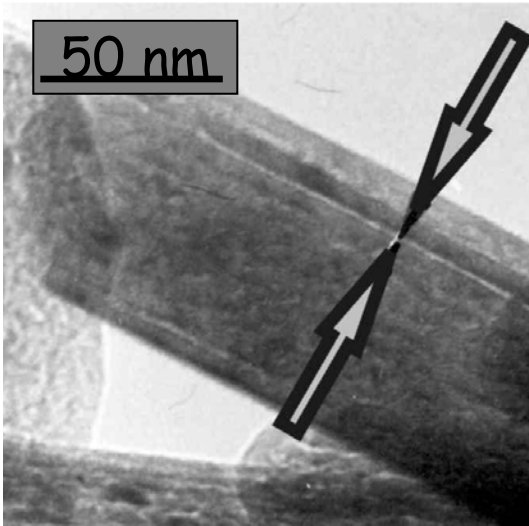
# Experimental and calculated x-ray diffraction patterns of turbostratic carbon



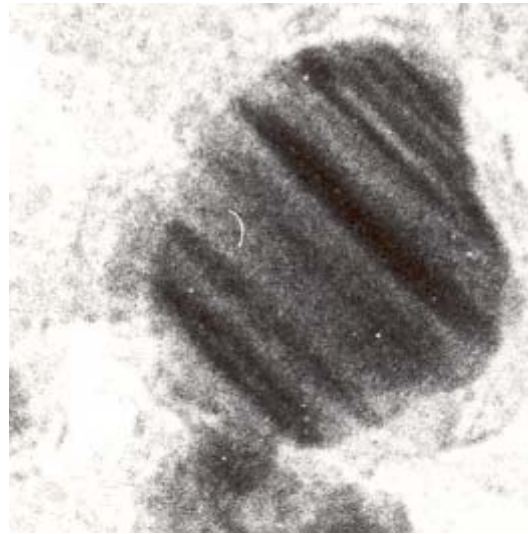
# Структура модифицированного гидроксида магния



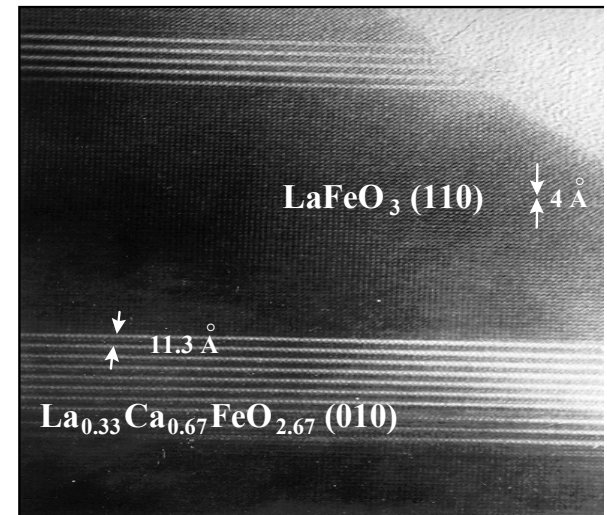
# 1D nanostructures



Planar Defects in hematite



1D nanostructure in metallic Co

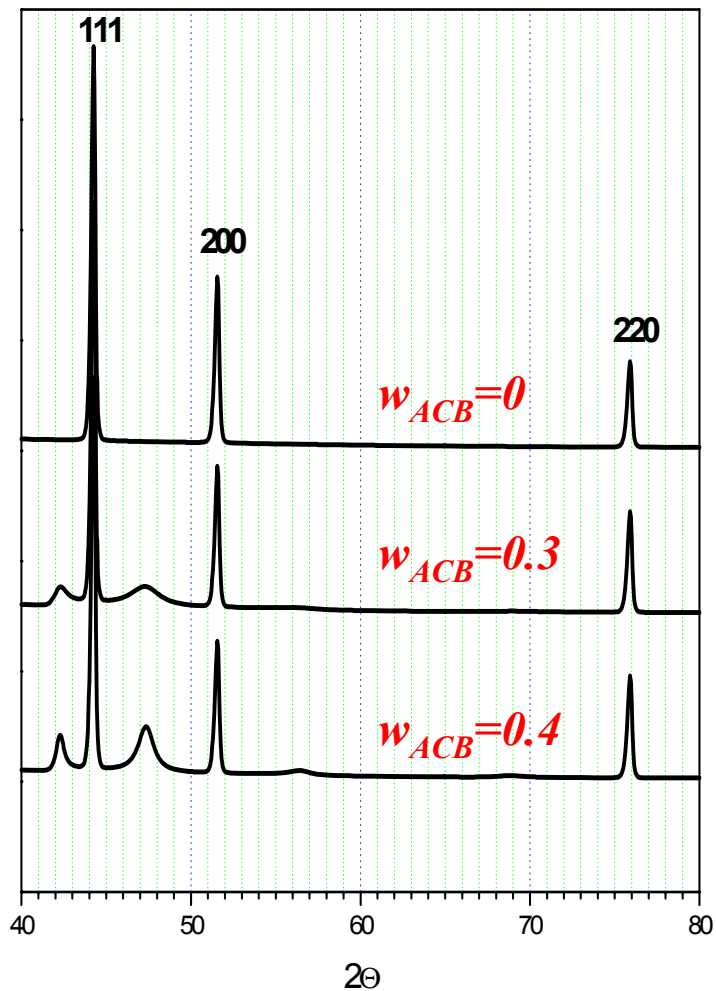


microdomains in  $\text{La}_{0.45}\text{Ca}_{0.55}\text{FeO}_{3-\delta}$

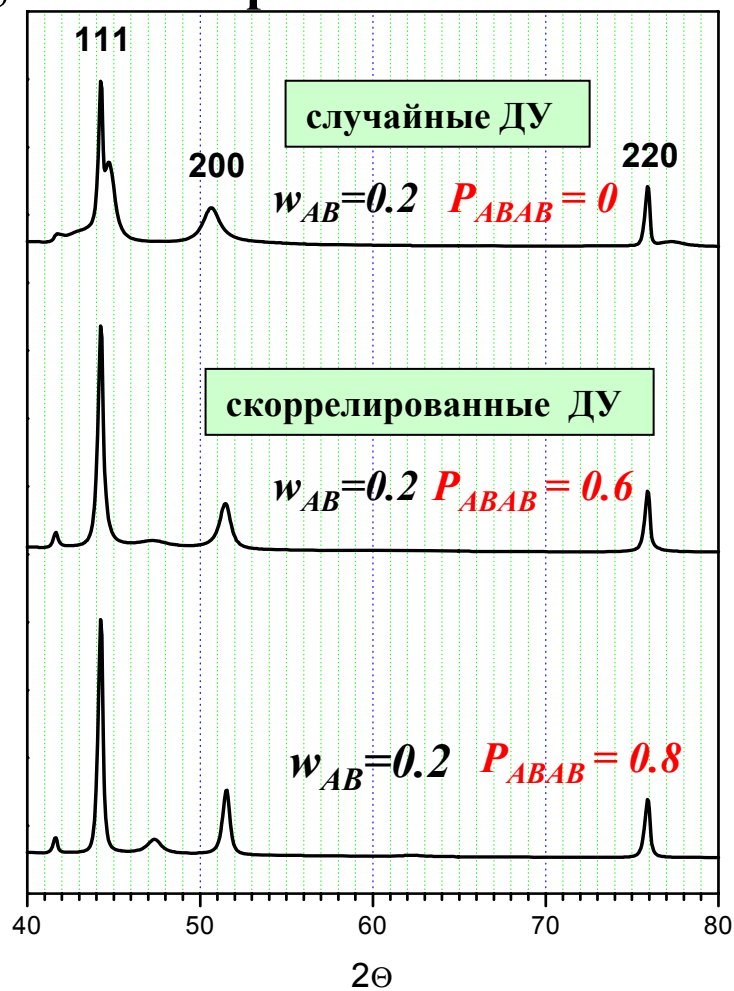


# Calculated diffraction patterns:

a - microtwins ABCACBABC, b - fcc-hcp coherent domains

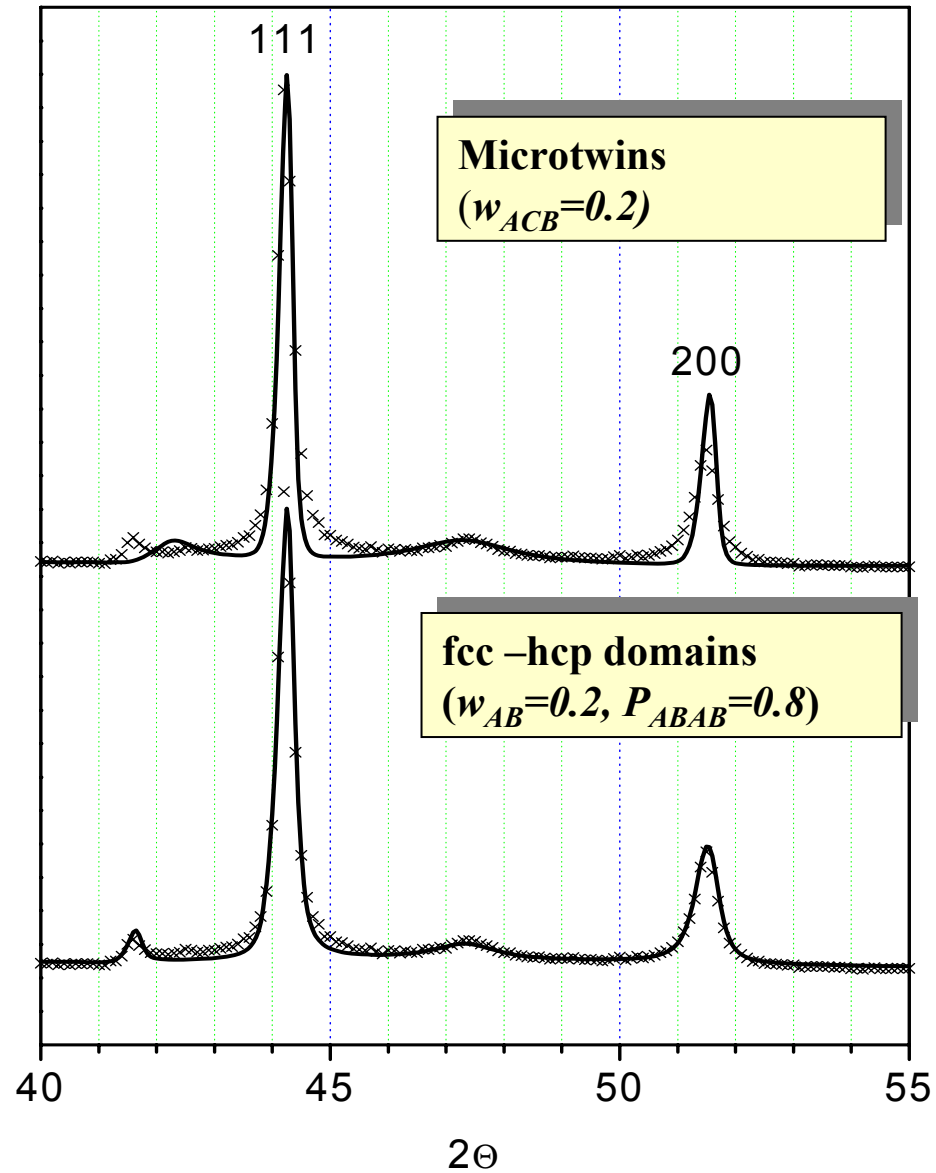


a



b

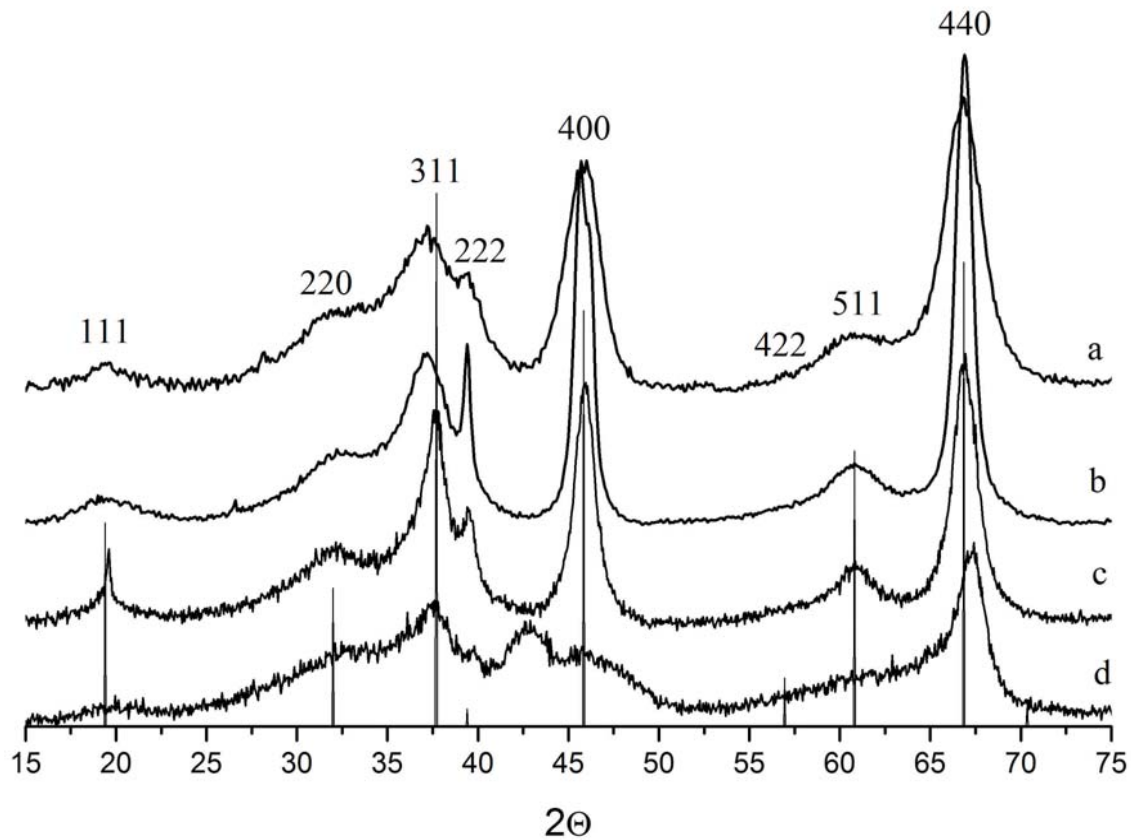
# Calculated and experimental x-ray diffraction patterns



# **КОГЕРЕНТНЫЕ 3D НАНОСТРУКТУРЫ:**

низкотемпературные формы оксида алюминия

# X-ray diffraction patterns of different alumina polymorphs



$\gamma\text{-Al}_2\text{O}_3$  from pseudoboehmite

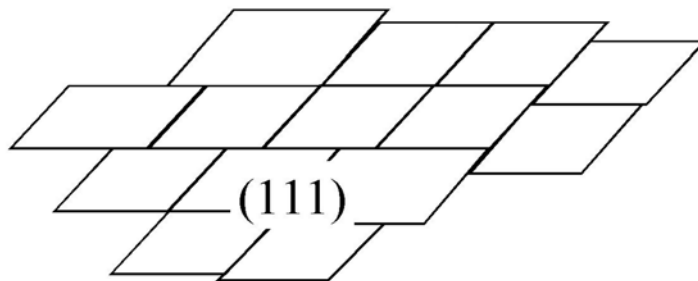
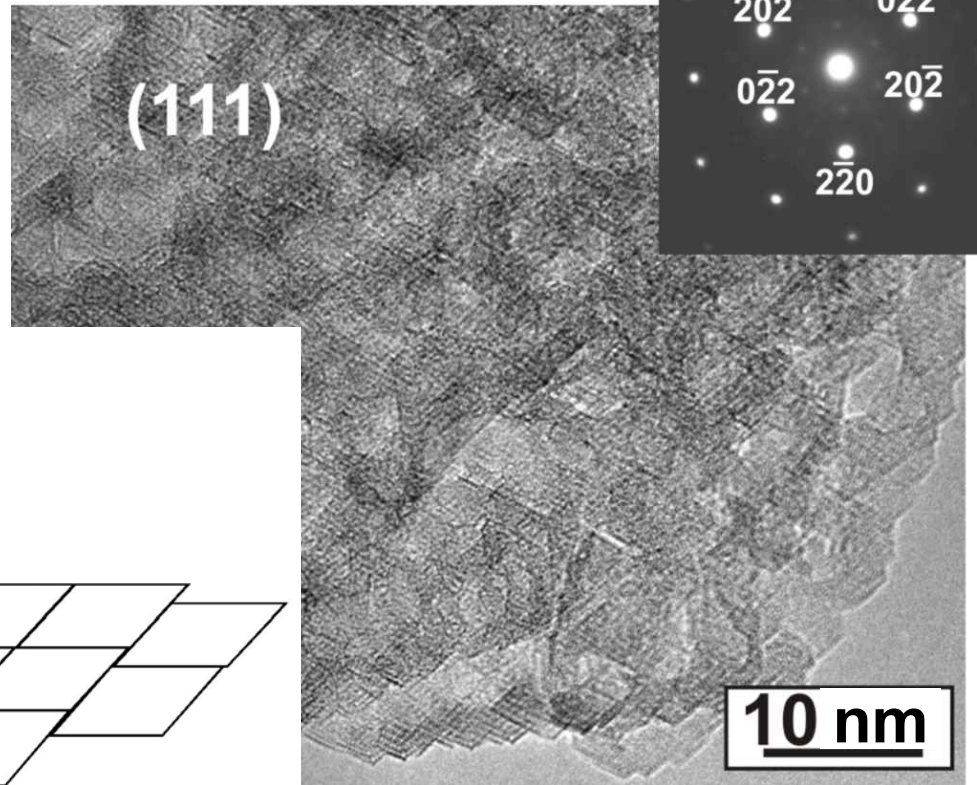
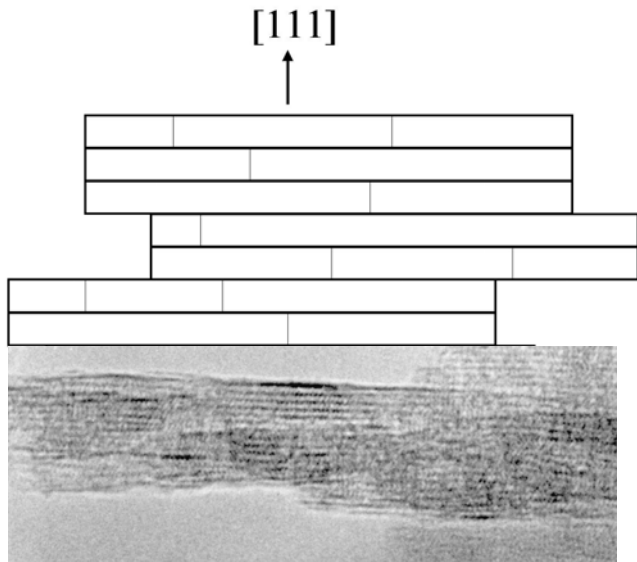
$\gamma\text{-Al}_2\text{O}_3$  from boehmite

$\eta\text{-Al}_2\text{O}_3$

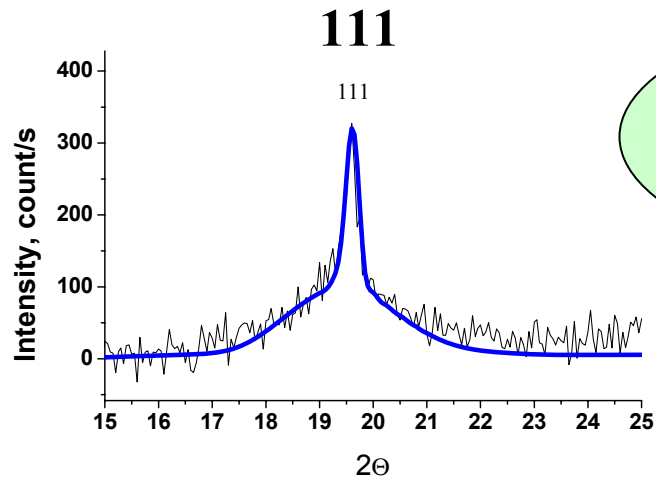
$\chi\text{-Al}_2\text{O}_3$

# Nanostructure of $\eta$ - $\text{Al}_2\text{O}_3$ prepared from bayerite

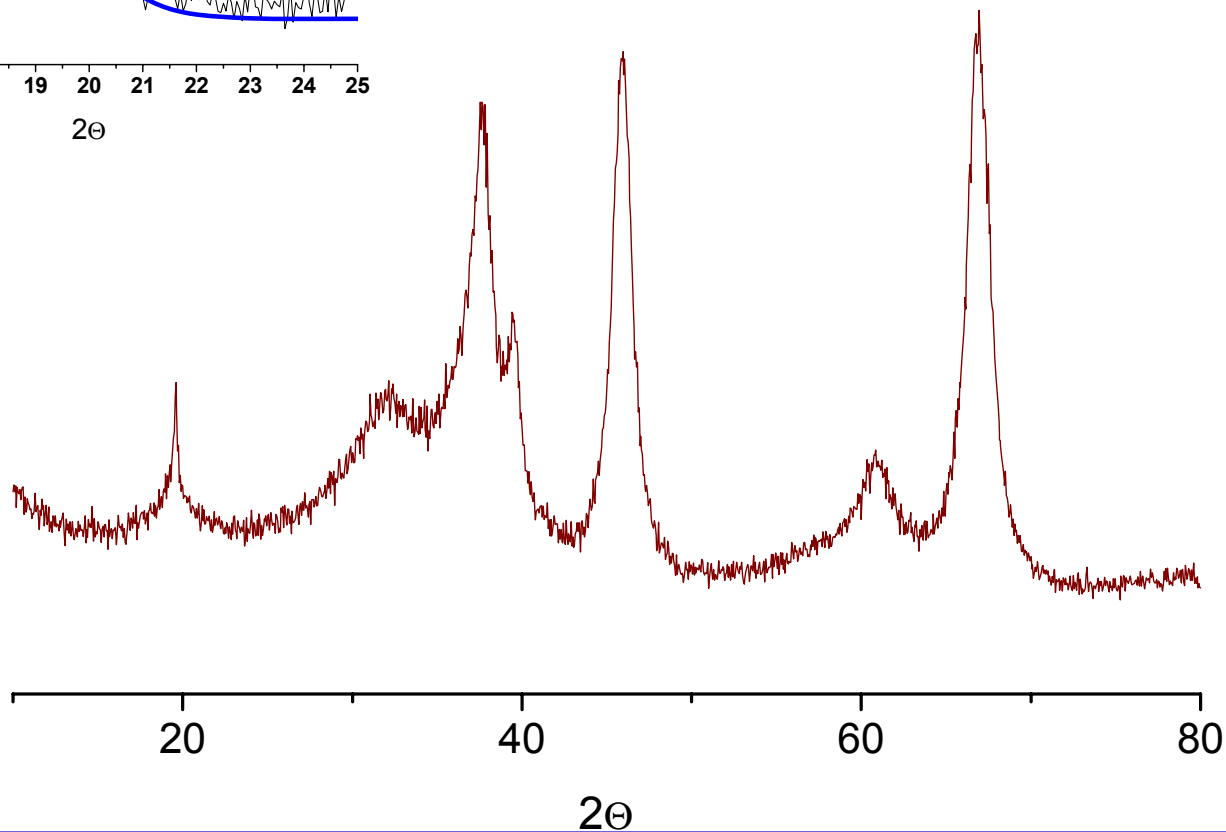
Side view of the platelet crystals



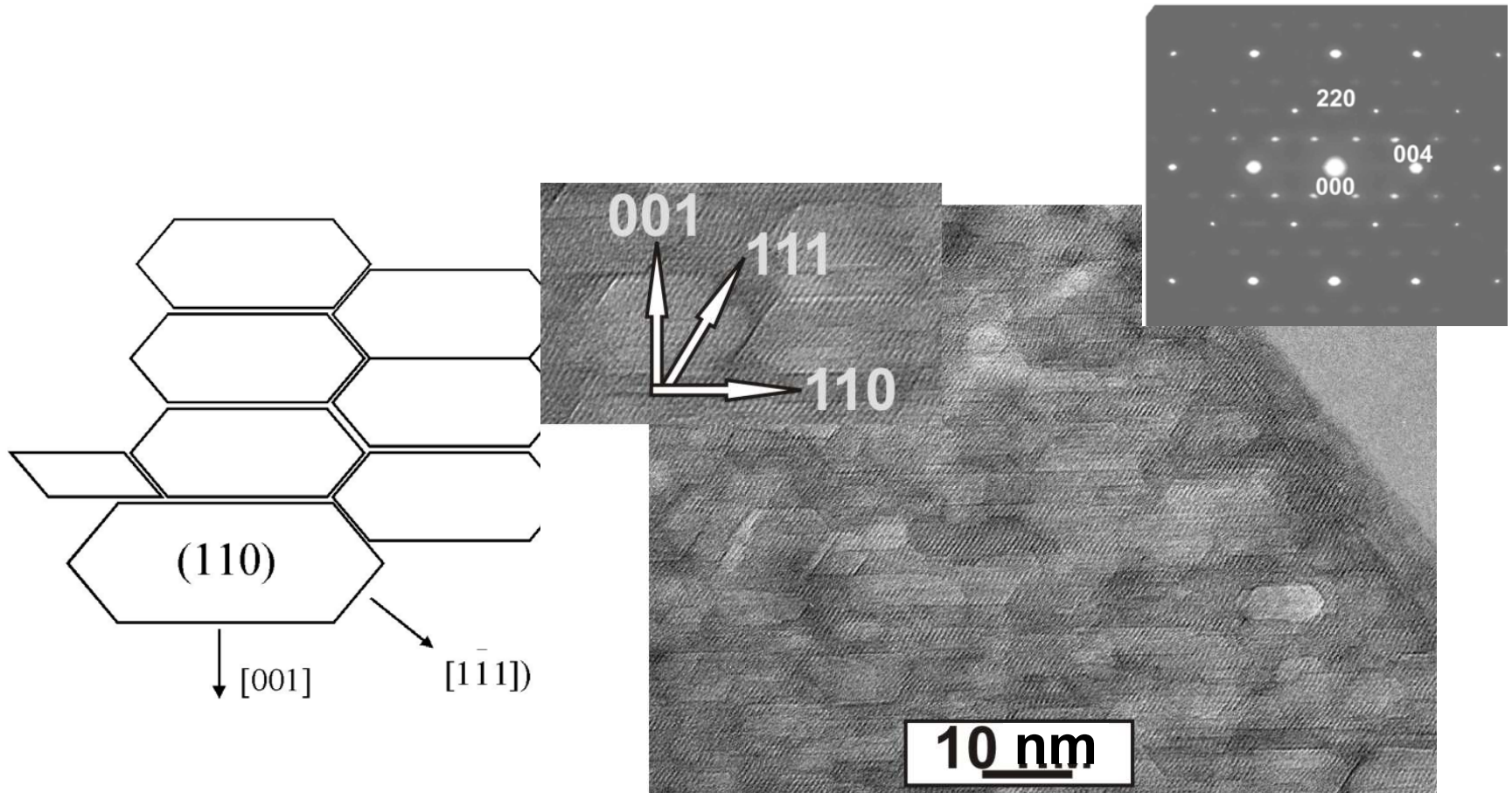
# $\eta\text{-Al}_2\text{O}_3$ : *111* peak



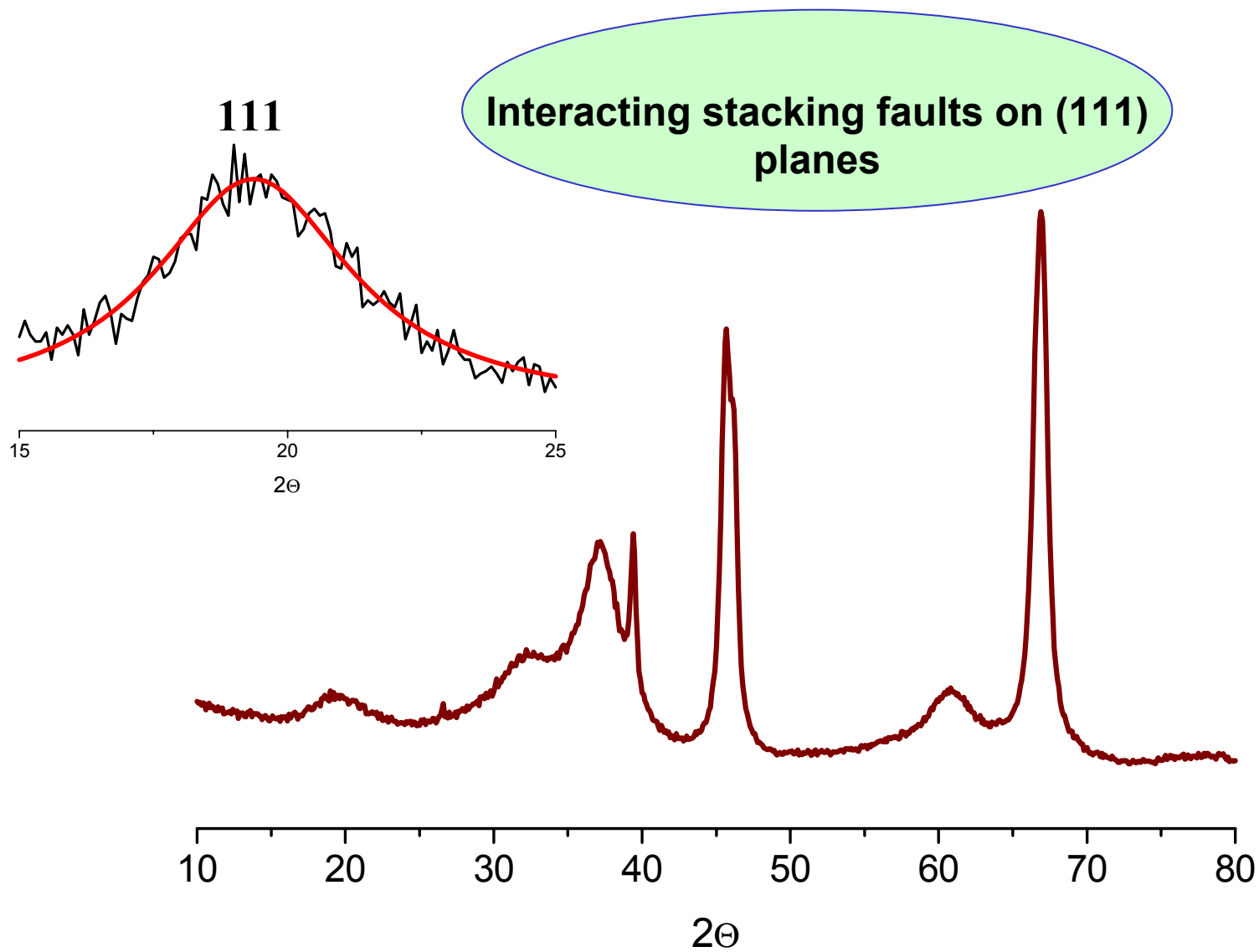
Stacking faults of  $(111)\frac{a}{4}[\bar{1}10]$  type



# Nanostructure of $\gamma\text{-Al}_2\text{O}_3$ prepared from boehmite

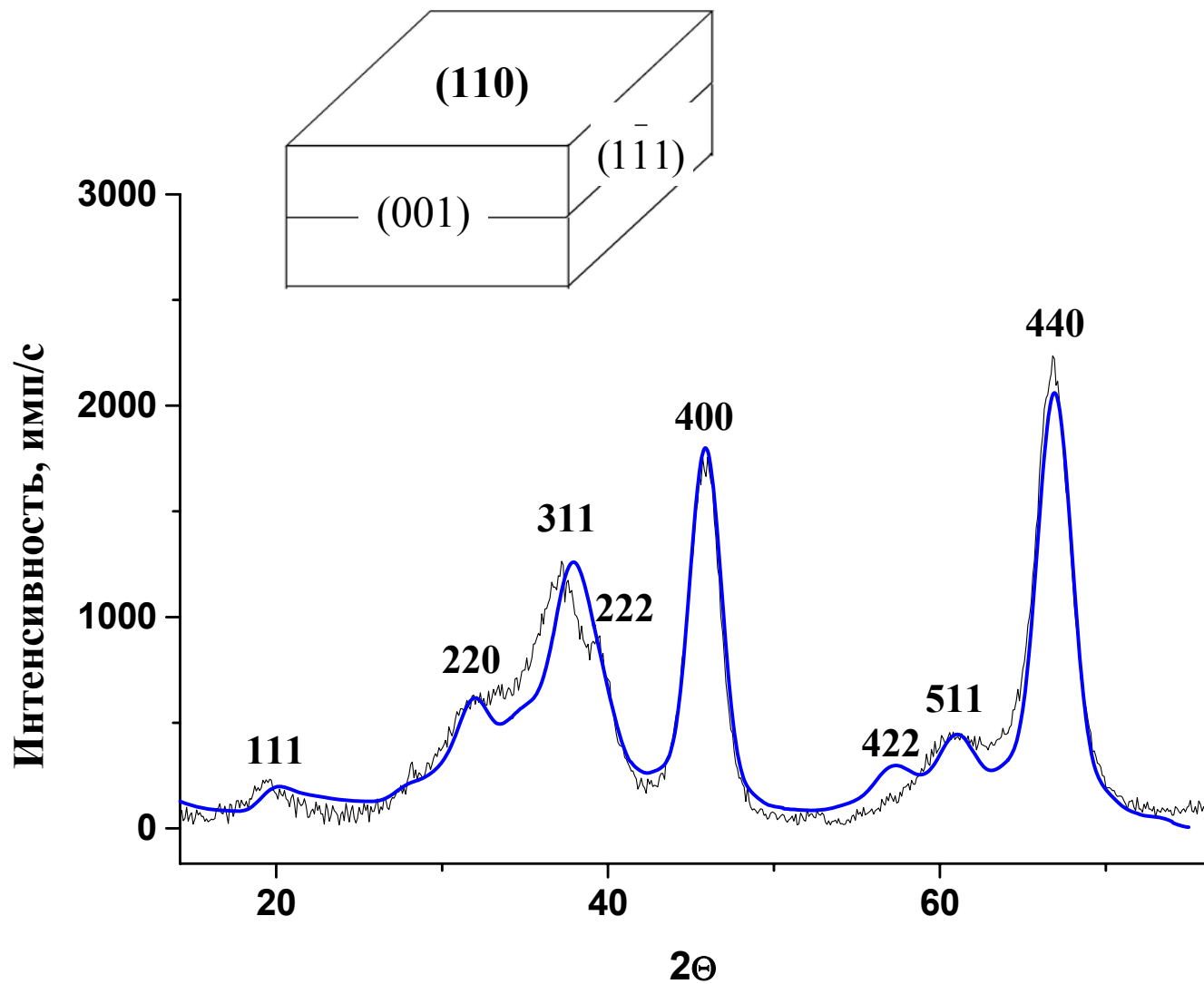


# $\gamma\text{-Al}_2\text{O}_3$ from boehmite: *shape of 111 reflection*

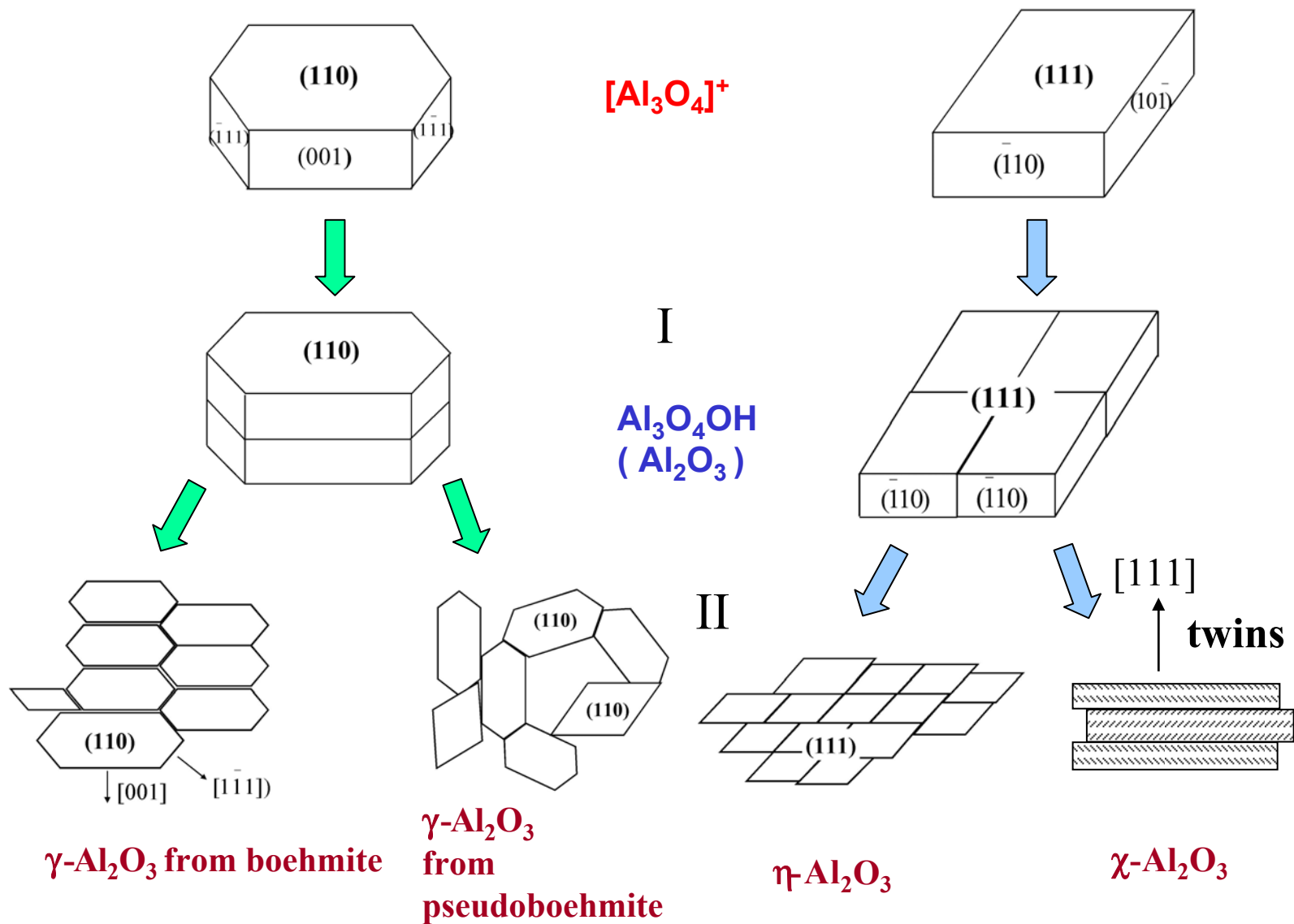




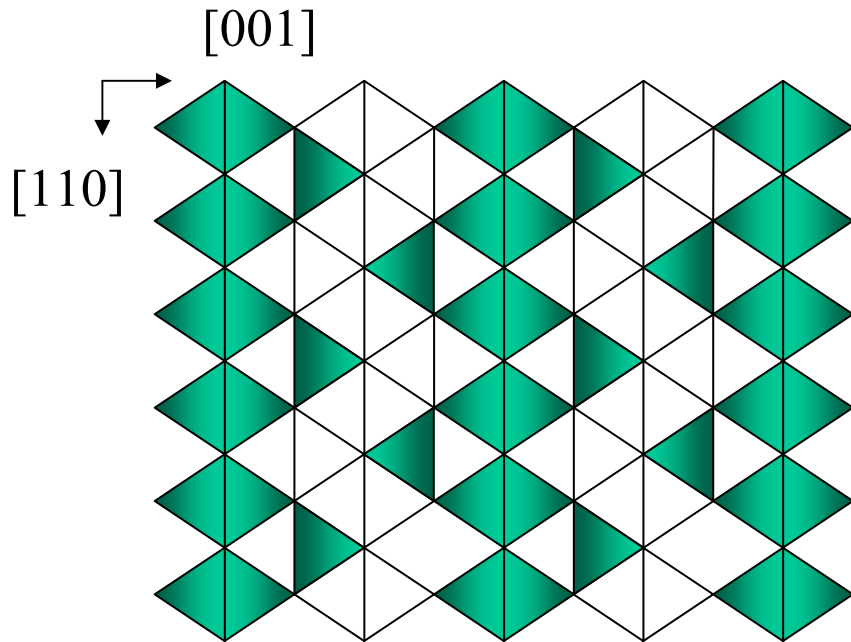
# Experimental and calculated (blue) diffraction patterns for $\gamma$ -Al<sub>2</sub>O<sub>3</sub> prepared from pseudoboehmite (R<sub>1</sub>=9.5%)



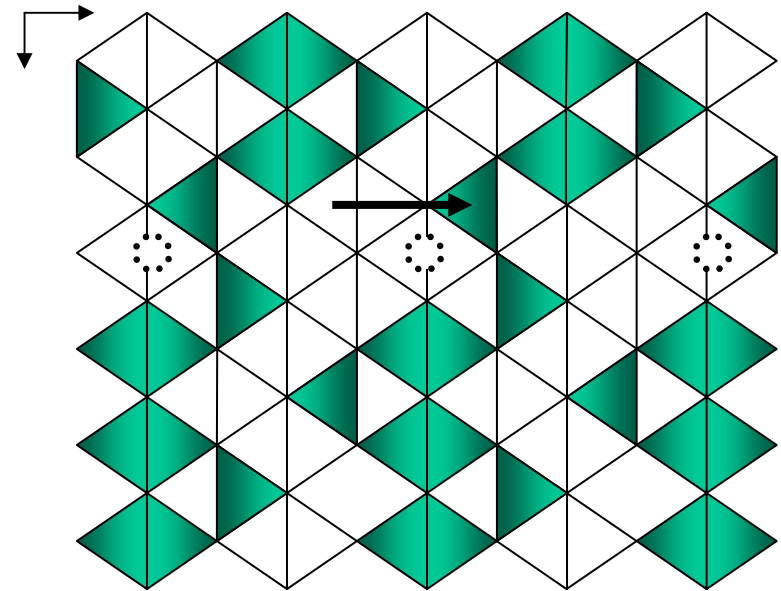
# Structural hierarchy in low temperature alumina polymorphs



# Atomic structure of stacking defect on (110) planes



*The regular spinel structure*



*The model of stacking faults*

# **X-ray diffraction analysis of nanocrystals:** *basic methods*

1. Rietveld method and modified algorithms based on the model of an infinite crystal
2. Debye Function Method
3. The calculation of the diffraction patterns from 1D distorted systems
4. Pair Distribution Function Method